

9/8/2019

Syllabus

B.Sc. (Hons) Mathematics



Department of Applied Mathematics
Gautam Buddha University

Document Version 1.1

Semester wise Details of B.Sc. (Hons.) Mathematics (BHM) Course & Credit Scheme
(wef. Session 2019-20)

Semester	S. No.	Course Code	Course Name	Nature	L	T	P	Credits
First	1	MT101/ MT105	Calculus/ Calculus Lab	C	4	0	2	6
	2	MT103	Algebra	C	5	1	0	6
	3	ES101	Environmental Studies	AECC	4	0	0	4
	4	GE-1	Generic Elective/Interdisciplinary	GE				6
Second	1	MT102	Real Analysis	C	5	1	0	6
	2	MT104/ MT 106	Differential Equations/ Differential Equations Lab	C	4	0	2	6
	3	EN105	Communicative English	AECC	4	0	0	4
	4	GE-2	Generic Elective/Interdisciplinary	GE				6
Third	1	MT201	Theory of Real Functions	C	5	1	0	6
	2	MT203	Group Theory-I	C	5	1	0	6
	3	MT205/ MT 209	Multivariate Calculus/ Multivariate Calculus Lab	C	4	0	2	6
	4	MT207	Latex and HTML	SEC	2	0	2	4
	5	GE-3	Generic Elective/Interdisciplinary	GE				6
Fourth	1	MT202/ MT 210	Partial Differential Equations/ PDE Lab	C	4	0	2	6
	2	MT204	Riemann Integration and Series of Functions	C	5	1	0	6
	3	MT206	Ring Theory and Linear Algebra-I	C	5	1	0	6
	4	MT208	Computer Algebra Systems and Related Software	SEC	2	0	2	4
	5	GE-4	Generic Elective/Interdisciplinary	GE				6
Fifth	1	MT301	Metric Spaces	C	5	1	0	6
	2	MT303	Group Theory-II	C	5	1	0	6
	3	DSE-1	DSE (including practical)	DSE	4	0	2	6
	4	DSE-2	DSE	DSE	5	1	0	6
Sixth	1	MT302/ MT 306	Complex Analysis/ Complex Analysis Lab	C	4	0	2	6
	2	MT304	Ring Theory and Linear Algebra-II	C	5	1	0	6
	3	DSE-3	DSE	DSE	5	1	0	6
	4	DSE-4	DSE	DSE	5	1	0	6
Total Credits								148

- 4 Hours lab will be taken as 2 hours labs in two slots.

List of Discipline Specific Elective (DSE) Courses:

DSE-1 (including practical): Any one of the following

- MT305/ MT 317 Numerical Analysis/ Lab
- MT307 /MT 319 Mathematical Modelling and Graph Theory/ Lab
- MT309 /MT 321 C++ Programming for Mathematics/ Lab

DSE-2: Any one of the following

- MT311 Probability Theory and Statistics
- MT313 Discrete Mathematics
- MT315 Cryptography and Network Security

DSE-3: Any one of the following

- MT306 Mathematical Finance
- MT308 Introduction to Information Theory and Coding
- MT310 Biomathematics

DSE-4: Any one of the following

- MT312 Number Theory
- MT314 Linear Programming and Applications
- MT316 Mechanics

Content Details

Bachelor of Mathematics (Hons.)

Semester I

Subject Code	MT101	Credit: 6 (L-T-P : 4-0-2) 4 Lecture (per week) 4 Hours Practical (per week per student)
Subject Name	Calculus	
Total Marks	150(Theory:70, Internal Assessment: 30, Practical: 50)	
Examination	3 Hours (Written) + 2 Hours (Practical)	

Unit 1: Derivatives for Graphing and Applications

(Lectures: 12)

The first-derivative test for relative extrema, Concavity and inflection points, Second-derivative test for relative extrema, Curve sketching using first and second derivative tests; Limits to infinity and infinite limits, Graphs with asymptotes, L'Hôpital's rule; Applications in Business, Economics and Life Sciences; Higher order derivatives, Leibniz rule.

Unit 2: Sketching and Tracing of Curves

(Lectures: 16)

Parametric representation of curves and tracing of parametric curves (except lines in \mathbb{R}^3), Polar coordinates and tracing of curves in polar coordinates; Techniques of sketching conics, Reflection properties of conics, Rotation of axes and second degree equations, Classification into conics using the discriminant.

Unit 3: Volume and Area of Surfaces

(Lectures: 16)

Volumes by slicing disks and method of washers, Volumes by cylindrical shells, Arc length, Arc length of parametric curves, Area of surface of revolution; Hyperbolic functions; Reduction formulae.

Unit 4: Vector Calculus and its Applications

(Lectures: 12)

Introduction to vector functions and their graphs, Operations with vector functions, Limits and continuity of vector functions, Differentiation and integration of vector functions; Modeling ballistics and planetary motion, Kepler's second law; Unit tangent, Normal and binormal vectors, Curvature.

References:

1. Anton, Howard, Bivens, Irl, & Davis, Stephen (2013). *Calculus* (10th ed.). John Wiley & Sons Singapore Pte. Ltd. Indian Reprint (2016) by Wiley India Pvt. Ltd. Delhi.
2. Osborne, George. A. (1906). *Differential and Integral Calculus with Examples and Applications*. Revised Edition. D. C. Heath & Co. Publishers. Boston, U.S.A.
3. Strauss, Monty J., Bradley, Gerald L., & Smith, Karl J. (2007). *Calculus* (3rd ed.). Dorling Kindersley (India) Pvt. Ltd. (Pearson Education). Delhi. Indian Reprint 2011.

Additional Reading:

1. Thomas, Jr. George B., Weir, Maurice D., & Hass, Joel (2014). *Thomas' Calculus* (13th ed.). Pearson Education, Delhi. Indian Reprint 2017.

Teaching Plan (Theory of MT101: Calculus):

Week 1: The first-derivative test for relative extrema, Concavity and inflection points, Second-derivative test for relative extrema, Curve sketching using first and second derivative tests.

[3] Chapter 4 (Section 4.3)

Week 2: Limits to infinity and infinite limits, Graphs with asymptotes, Vertical tangents and cusps, L'Hôpital's rule.

[3] Chapter 4 (Sections 4.4, and 4.5)

Week 3: Applications of derivatives in Business, Economics and Life sciences. Higher order derivatives and Leibniz rule for higher order derivatives for the product of two functions.

[3] Chapter 4 (Section 4.7)

[2] Chapter IV (Sections 57 to 60)

Week 4: Parametric representation of curves and tracing of parametric curves (except lines in \mathbb{R}^3), Polar coordinates and the relationship between Cartesian and polar coordinates.

[3] Chapter 9 [Section 9.4 (pages 471 to 475)]

[2] Chapter 10 (Sections 10.1, 10.2, up to Example 2, page 707)

Weeks 5 and 6: Tracing of curves in polar coordinates. Techniques of sketching conics: Parabola, Ellipse and Hyperbola.

[1] Chapter 10 [Sections 10.2 (page 707 to 717), and 10.4 up to Example 10 page 742)]

Week 7: Reflection properties of conics, Rotation of axes, Second degree equations and their classification into conics using the discriminant.

[1] Chapter 10 [Sections 10.4 (page 742 to 744), and 10.5]

Weeks 8 and 9: Volumes by slicing disks and method of washers, Volumes by cylindrical shells, Arc length, Arc length of parametric curves.

[1] Chapter 5 (Sections 5.2, 5.3, and 5.4)

Week 10: Area of surface of revolution; Hyperbolic functions.

[1] Chapter 5 (Section 5.5), and Chapter 6 (Section 6.8)

Week 11: Reduction formulae, and to obtain the iterative formulae for the integrals of the form:

$$\int \sin^n x dx, \int \cos^n x dx, \int \tan^n x dx, \int \sec^n x dx, \text{ and } \int \sin^m x \cos^n x dx.$$

[1] Chapter 7 [Sections 7.2, and 7.3 (pages 497 to 503)]

Week 12: Introduction to vector functions and their graphs, Operations with vector functions, Limits and continuity of vector functions, Differentiation and tangent vectors.

[3] Chapter 10 (Sections 10.1, and 10.2 up to page 504)

Week 13: Properties of vector derivatives and integration of vector functions; Modeling ballistics and planetary motion, Kepler's second law.

[3] Chapter 10 (Sections 10.2 (pages 505 to 511), and 10.3)

Week 14: Unit tangent, Normal and binormal vectors, Curvature.

[1] Chapter 12 (Sections 12.4, and 12.5)

Practical / Lab work to be performed in Computer Lab.

List of the practical to be done using Mathematica /MATLAB /Maple /Scilab/Maxima etc.

- (i) Plotting the graphs of the following functions: ax , $[x]$ (greatest integer function), $\sqrt{ax+b}$, $|ax+b|$, $c \pm |ax+b|$, $x^{\pm n}$, $x^{1/n}$ ($n \in \mathbb{Q}$)
 $|x|/x$, $\sin(1/x)$, $x \sin(1/x)$, and $e^{\pm 1/x}$ for $x \neq 0$.
 e^{ax+b} , $\log(ax+b)$, $1/(ax+b)$, $\sin(ax+b)$, $\cos(ax+b)$, $|\sin(ax+b)|$, $|\cos(ax+b)|$.
 Observe and discuss the effect of changes in the real constants a , b and c on the graphs
- (ii) Plotting the graphs of polynomial of degree 4 and 5, and their first and second derivatives, and analysis of these graphs in context of the concepts covered in Unit 1.
- (iii) Sketching parametric curves, e.g., Trochoid, Cycloid, Epicycloid and Hypocycloid.
- (iv) Tracing of conic in Cartesian coordinates.
- (v) Obtaining surface of revolution of curves.
- (vi) Graph of hyperbolic functions.
- (vii) Computation of limit, Differentiation, Integration and sketching of vector-valued functions.
- (viii) Complex numbers and their representations, Operations like addition, Multiplication, Division, Modulus. Graphical representation of polar form.
- (ix) Find numbers between two real numbers and plotting of finite and infinite subset of \mathbb{R} .
- (x) **Matrix Operations:** Addition, Multiplication, Inverse, Transpose, Determinant, Rank, Eigenvectors, Eigenvalues, Characteristic equation and verification of the Cayley-Hamilton theorem, Solving the systems of linear equations.

Subject Code	MT103	Credit: 6 (L-T-P : 5-1-0)
Subject Name	Algebra	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Theory of Equations and Complex Numbers (Lectures: 20)

Elementary theorems on the roots of an equation, Polynomials, The remainder and factor theorem, Synthetic division, Factored form of a polynomial, The Fundamental theorem of algebra, Relations between the roots and the coefficients of polynomial equations, Imaginary roots occur in pairs, Integral and rational roots; Polar representation of complex numbers, The n th roots of unity, DeMoivre's theorem for integer and rational indices and its applications.

Unit 2: Equivalence Relations and Functions (Lectures: 10)

Equivalence relations, Functions, Composition of functions, Invertibility and inverse of functions, One-to-one correspondence and the cardinality of a set.

Unit 3: Basic Number Theory (Lectures: 10)

The division algorithm, Divisibility and the Euclidean algorithm, The fundamental theorem of arithmetic, Modular arithmetic and basic properties of congruences; Principles of mathematical induction and well ordering principle.

Unit 4: Row Echelon Form of Matrices and Applications (Lectures: 30)

Systems of linear equations, Row reduction and echelon forms, Vector equations, The matrix equation $A\mathbf{x} = \mathbf{b}$, Solution sets of linear systems, Linear independence, The rank of a matrix and applications; Introduction to linear transformations, The matrix of a linear transformation; Matrix operations, The inverse of a matrix, Characterizations of invertible matrices, Applications to Computer Graphics, Eigenvectors and eigenvalues, The characteristic equation and the Cayley-Hamilton theorem.

References:

1. Andreescu, Titu & Andrica Dorin. (2014). *Complex Numbers from A to...Z*. (2nd ed.). Birkhäuser.
2. Dickson, Leonard Eugene (1922). *First Course in The Theory of Equations*. John Wiley & Sons, Inc. New York. The Project Gutenberg EBook.
3. Goodaire, Edgar G., & Parmenter, Michael M. (2005). *Discrete Mathematics with Graph Theory* (3rd ed.). Pearson Education Pvt. Ltd. Indian Reprint 2015.
4. Kolman, Bernard, & Hill, David R. (2001). *Introductory Linear Algebra with Applications* (7th ed.). Pearson Education, Delhi. First Indian Reprint 2003.
5. Lay, David C., Lay, Steven R., & McDonald, Judi J. (2016). *Linear Algebra and its Applications* (5th ed.). Pearson Education

Additional Readings:

1. Andrilli, Stephen, & Hecker, David (2016). *Elementary Linear Algebra* (5th ed.). Academic Press, Elsevier India Private Limited.
2. Burton, David M. (2007). *Elementary Number Theory* (7th ed.). Tata Mc-Graw Hill Edition, Indian Reprint.

Teaching Plan (MT103: Algebra):

Weeks 1 and 2: Elementary theorems on the roots of an equation, Polynomials, The remainder and factor theorem, Synthetic division, Factored form of a polynomial, The Fundamental theorem of algebra, Relations between the roots and the coefficients of polynomial equations, Imaginary roots occur in pairs, Integral and rational roots.

[2] Chapter II (Sections 12 to 16, 19 to 21, 24 and 27, Statement of the Fundamental theorem of algebra)

Weeks 3 and 4: Polar representation of complex numbers, n th roots of unity, DeMoivre's theorem for integer and rational indices and its applications.

[1] Chapter 2

Weeks 5 and 6: Equivalence relations, Functions, Composition of functions, Invertibility and inverse of functions, One-to-one correspondence and the cardinality of a set.

[3] Chapter 2 (Section 2.4), and Chapter 3

Weeks 7 and 8: The division algorithm, Divisibility and the Euclidean algorithm, The fundamental theorem of arithmetic (statement only), Modular arithmetic and basic properties of congruences. Principles of mathematical induction and well ordering principle.

[3] Chapter 4 [Sections 4.1 up to 4.1.6, 4.2 up to 4.2.11, 4.3 (4.3.7 to 4.3.9), and 4.4 up to 4.4.8], and Chapter 5 (Sections 5.1.1 and 5.1.4)

Weeks 9 and 10: Systems of linear equations, Row reduction and echelon forms, Vector equations, The matrix equation $A\mathbf{x} = \mathbf{b}$, Solution sets of linear systems, Linear independence, The rank of a matrix and applications (Definition and examples).

[5] Chapter 1 (Sections 1.1 to 1.5)

[4] Chapter 6 [Section 6.6 (pages 287 to 291)]

Week 11: Introduction to linear transformations, The matrix of a linear transformation. [5] Chapter 1 (Sections 1.7 to 1.9)

Weeks 12 and 13: Matrix operations, The inverse of a matrix, Characterizations of invertible matrices, Applications to Computer Graphics.

[5] Chapter 2 (Sections 2.1 to 2.3, and 2.7 up to Example 6, page 142)

Week 14: Eigenvectors and eigenvalues, The characteristic equation and the Cayley-Hamilton theorem.

[4] Chapter 5 (Sections 5.1 and 5.2, Supplementary exercises 5 and 7, page 328)

Semester II

Subject Code	MT102	Credit: 6 (L-T-P : 5-1-0)
Subject Name	Real Analysis	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Real Number SystemR

(Lectures: 10)

Algebraic and order properties of \mathbb{R} , Absolute value of a real number; Bounded above and bounded below sets, Supremum and infimum of a nonempty subset of \mathbb{R} .

Unit 2: Properties of \mathbb{R}

(Lectures: 10)

The completeness property of \mathbb{R} , Archimedean property, Density of rational numbers in \mathbb{R} , Definition and types of intervals, Nested intervals property; Neighborhood of a point in Open and closed sets in \mathbb{R} .

Unit 3: Sequences in \mathbb{R}

(Lectures: 25)

Convergent sequence, Limit of a sequence, Bounded sequence, Limit theorems, Monotone sequences, Monotone convergence theorem, Subsequences, Bolzano-Weierstrass theorem for sequences, Limit superior and limit inferior for bounded sequence, Cauchy sequence, Cauchy's convergence criterion.

Unit 4: Infinite Series

(Lectures: 25)

Convergence and divergence of infinite series of real numbers, Necessary condition for convergence, Cauchy criterion for convergence; Tests for convergence of positive term series: Integral test, Basic comparison test, Limit comparison test, D'Alembert's ratio test, Cauchy's n th root test; Alternating series, Leibniz test, Absolute and conditional convergence.

References:

1. Bartle, Robert G., & Sherbert, Donald R. (2015). *Introduction to Real Analysis* (4th ed.). Wiley India Edition. New Delhi.
2. Bilodeau, Gerald G., Thie, Paul R., & Keough, G. E. (2010). *An Introduction to Analysis* (2nd ed.). Jones and Bartlett India Pvt. Ltd. Student Edition. Reprinted 2015.
3. Denlinger, Charles G. (2011). *Elements of Real Analysis*. Jones and Bartlett India Pvt. Ltd. Student Edition. Reprinted 2015.

Additional Readings:

1. Ross, Kenneth A. (2013). *Elementary Analysis: The theory of calculus* (2nd ed.). Undergraduate Texts in Mathematics, Springer. Indian Reprint.
2. Thomson, Brian S., Bruckner, Andrew. M., & Bruckner, Judith B. (2001). *Elementary Real Analysis*. Prentice Hall.

Teaching Plan (Theory of MT102: Real Analysis):

Weeks 1 and 2: Algebraic and order properties of \mathbb{R} . Absolute value of a real number; Bounded above and bounded below sets, Supremum and infimum of a nonempty subset of \mathbb{R} .
[1] Chapter 2 [Sections 2.1, 2.2 (2.2.1 to 2.2.6), and 2.3 (2.3.1 to 2.3.5)]

Weeks 3 and 4: The completeness property of \mathbb{R} , Archimedean property, Density of rational numbers in \mathbb{R} , Definition and types of intervals, Nested intervals property; Neighborhood of a point in \mathbb{R} , Open and closed sets in \mathbb{R} .
[1] Chapter 2 [Sections 2.3 (2.3.6), 2.4 (2.4.3 to 2.4.9), and 2.5 up to Theorem 2.5.3]
[1] Chapter 11 [Section 11.1 (11.1.1 to 11.1.3)]

Weeks 5 and 6: Sequences and their limits, Bounded sequence, Limit theorems.
[1] Chapter 3 (Sections 3.1 and 3.2)

Week 7: Monotone sequences, Monotone convergence theorem and applications.
[1] Chapter 3 (Section 3.3)

Week 8: Subsequences and statement of the Bolzano-Weierstrass theorem. Limit superior and limit inferior for bounded sequence of real numbers with illustrations only.
[1] Chapter 3 [Section 3.4 (3.4.1 to 3.4.12), except 3.4.4, 3.4.7, 3.4.9 and 3.4.11]

Week 9: Cauchy sequences of real numbers and Cauchy's convergence criterion.
[1] Chapter 3 [Section 3.5 (3.5.1 to 3.5.6)]

Week 10: Convergence and divergence of infinite series, Sequence of partial sums of infinite series, Necessary condition for convergence, Cauchy criterion for convergence of series.
[3] Chapter 8 (Section 8.1)

Weeks 11 and 12: Tests for convergence of positive term series: Integral test statement and convergence of p -series, Basic comparison test, Limit comparison test with applications, D'Alembert's ratio test and Cauchy's n th root test.
[3] Chapter 8 (Section 8.2 up to 8.2.19)

Weeks 13 and 14: Alternating series, Leibniz test, Absolute and conditional convergence. [2] Chapter 6 (Section 6.2)

Subject Code	MT104	Credit: 6 (L-T-P : 4-0-2) 4 Lecture (per week) 4 Hours Practical (per week per student)
Subject Name	Differential Equations	
Total Marks	150(Theory:70, Internal Assessment: 30, Practical: 50)	
Examination	3 Hours (Written) + 2 Hours (Practical)	

Unit 1: Differential Equations and Mathematical Modeling (Lectures: 12)

Differential equations and mathematical models, Order and degree of a differential equation, Exact differential equations and integrating factors of first order differential equations, Reducible second order differential equations, Application of first order differential equations to equations to acceleration-velocity model, Growth and decay model.

Unit 2: Population Growth Models (Lectures: 12)

Introduction to compartmental models, Lake pollution model (with case study of Lake Burley Griffin), Drug assimilation into the blood (case of a single cold pill, case of a course of cold pills, case study of alcohol in the bloodstream), Exponential growth of population, Limited growth of population, Limited growth with harvesting.

Unit 3: Second and Higher Order Differential Equations (Lectures: 20)

General solution of homogeneous equation of second order, Principle of superposition for a homogeneous equation; Wronskian, its properties and applications, Linear homogeneous and non-homogeneous equations of higher order with constant coefficients, Euler's equation, Method of undetermined coefficients, Method of variation of parameters, Applications of second order differential equations to mechanical vibrations.

Unit 4: Analysis of Mathematical Models (Lectures: 12)

Interacting population models, Epidemic model of influenza and its analysis, Predator-prey model and its analysis, Equilibrium points, Interpretation of the phase plane, Battle model and its analysis.

References:

1. Barnes, Belinda & Fulford, Glenn R. (2015). *Mathematical Modelling with CaseStudies, Using Maple and MATLAB* (3rd ed.). CRC Press, Taylor & Francis Group.
2. Edwards, C. Henry, Penney, David E., &Calvis, David T. (2015). *Differential Equationand Boundary Value Problems: Computing and Modeling* (5th ed.). Pearson Education.
3. Ross, Shepley L. (2004). *Differential Equations* (3rd ed.). John Wiley & Sons. India

Teaching Plan (Theory of MT104: Differential Equations):

Weeks 1 and 2: Differential equations and mathematical models, Order and degree of a differentialequation, Exact differential equations and integrating factors of first order differential equations, Reducible second order differential equations.

[2] Chapter 1 (Sections 1.1, and 1.6)

[3] Chapter 2.

Week 3: Application of first order differential equations to equations to acceleration-velocity model, Growth and decay model.

[2] Chapter 1 (Section 1.4, pages 35 to 38), and Chapter 2 (Section 2.3)

[3] Chapter 3 (Section 3.3, A and B with Examples 3.8, 3.9)

Week 4: Introduction to compartmental models, Lake pollution model (with case study of Lake BurleyGriffin).

[1] Chapter 2 (Sections 2.1, 2.5, and 2.6)

Week 5: Drug assimilation into the blood (case of a single cold pill, case of a course of cold pills, Casestudy of alcohol in the bloodstream).

[1] Chapter 2 (Sections 2.7, and 2.8)

Week 6: Exponential growth of population, Density dependent growth, Limited growth withharvesting.

[1] Chapter 3 (Sections 3.1 to 3.3)

Weeks 7 to 9: General solution of homogeneous equation of second order, Principle of superpositionfor a homogeneous equation; Wronskian, its properties and applications; Linear homogeneous and non-homogeneous equations of higher order with constant coefficients; Euler's equation.

[2] Chapter 3 (Sections 3.1 to 3.3)

Weeks 10 and 11: Method of undetermined coefficients, Method of variation of parameters;Applications of second order differential equations to mechanical vibrations.

[2] Chapter 3 (Sections 3.4 (pages 172 to 177), and 3.5)

Weeks 12 to 14: Interacting population models, Epidemic model of influenza and its analysis, Predator-prey model and its analysis, Equilibrium points, Interpretation of the phase plane, Battle model and its analysis.

[1] Chapter 5 (Sections 5.1, 5.2, 5.4, and 5.9), and Chapter 6 (Sections 6.1 to 6.4).

Differential Equation Lab

Modeling of the following problems using Mathematica /MATLAB/Maple/Maxima/Scilab etc.

1. Plotting of second and third order respective solution family of differential equation.
2. Growth and decay model (exponential case only).
3. (a) Lake pollution model (with constant/seasonal flow and pollution concentration).
(b) Case of single cold pill and a course of cold pills.
(c) Limited growth of population (with and without harvesting).
4. (a) Predatory-prey model (basic volterra model, with density dependence, effect of DDT, two prey one predator).
(b) Epidemic model of influenza (basic epidemic model, contagious for life, disease with carriers).
(c) Battle model (basic battle model, jungle warfare, long range weapons).
5. Plotting of recursive sequences, and study the convergence.
6. Find a value $m \in \mathbb{N}$ that will make the following inequality holds for all $n > m$:
(i) $|\sqrt[n]{0.5} - 1| < 10^{-3}$ (ii) $|\sqrt[n]{n} - 1| < 10^{-3}$
(iii) $(0.9)^n < 10^{-3}$ (iv) $2^n / n! < 10^{-7}$
7. Verify the Bolzano-Weierstrass theorem through plotting of sequences and hence identify convergent subsequences from the plot.
8. Study the convergence/divergence of infinite series of real numbers by plotting their sequences of partial sum.
9. Cauchy's root test by plotting n th roots.
10. D'Alembert's ratio test by plotting the ratio of n th and $(n+1)$ th term of the given series of positive terms.
11. For the following sequences $\langle a_n \rangle$, given $\varepsilon = 1/2^k$, $p = 10^j$, $k = 0, 1, 2, \dots$; $j = 1, 2, 3, \dots$
Find $m \in \mathbb{N}$ such that (i) $|a_{m+p} - a_m| < \varepsilon$, (ii) $|a_{2m+p} - a_{2m}| < \varepsilon$, where a_n is given as:
(a) $\frac{n+1}{n}$ (b) $\frac{1}{n}$ (c) $1 - \frac{1}{2} + \frac{1}{3} - \dots + \frac{(-1)^{n-1}}{n}$
(d) $\frac{(-1)^n}{n}$ (e) $2^{-n} n^2$ (f) $1 + \frac{1}{2!} + \dots + \frac{1}{n!}$
12. For the following series $\sum a_n$, calculate (i) $\left| \frac{a_{n+1}}{a_n} \right|$, (ii) $|a_n|^{1/n}$, for $n = 10^j$, $j = 1, 2, 3, \dots$

and identify the convergent series, where a_n is given as:

- (a) $\left(\frac{1}{n}\right)^{1/n}$, (b) $\frac{1}{n}$, (c) $\frac{1}{n^2}$, (d) $\left(1 + \frac{1}{\sqrt{n}}\right)^{-n^{3/2}}$, (e) $\frac{n!}{n^n}$
(f) $\frac{n^3 + 5}{3^n + 2}$, (g) $\frac{1}{n^2 + n}$, (h) $\frac{1}{\sqrt{n+1}}$, (i) $\cos n$, (j) $\frac{1}{n \log n}$, (k) $\frac{1}{n(\log n)^2}$

Semester III

Subject Code	MT201	Credit: 6 (L-T-P : 5-1-0)
Subject Name	Theory of Real Functions	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Limits of Functions

(Lectures: 15)

Limits of functions ($\varepsilon - \delta$ approach), Sequential criterion for limits, Divergence criteria, Limit theorems, One-sided limits, Infinite limits and limits at infinity.

Unit 2: Continuous Functions and their Properties

(Lectures: 25)

Continuous functions, Sequential criterion for continuity and discontinuity, Algebra of continuous functions, Properties of continuous functions on closed and bounded intervals; Uniform continuity, Non-uniform continuity criteria, Uniform continuity theorem.

Unit 3: Derivability and its Applications

(Lectures: 20)

Differentiability of a function, Algebra of differentiable functions, Carathéodory's theorem and chain rule; Relative extrema, Interior extremum theorem, Rolle's theorem, Mean-value theorem and its applications, Intermediate value property of derivatives - Darboux's theorem.

Unit 4: Taylor's Theorem and its Applications

(Lectures: 10)

Taylor polynomial, Taylor's theorem with Lagrange form of remainder, Application of Taylor's theorem in error estimation; Relative extrema, and to establish a criterion for convexity; Taylor's series expansions of e^x , $\sin x$ and $\cos x$.

Reference:

1. Bartle, Robert G., & Sherbert, Donald R. (2015). *Introduction to Real Analysis* (4th ed.). Wiley India Edition. New Delhi.

Additional Readings:

1. Ghorpade, Sudhir R. & Limaye, B. V. (2006). *A Course in Calculus and Real Analysis*. Undergraduate Texts in Mathematics, Springer (SIE). First Indian reprint.
2. Mattuck, Arthur. (1999). *Introduction to Analysis*, Prentice Hall.
3. Ross, Kenneth A. (2013). *Elementary Analysis: The theory of calculus* (2nd ed.). Undergraduate Texts in Mathematics, Springer. Indian Reprint.

Teaching Plan (Theory of MT201: Theory of Real Functions):

Week 1: Definition of the limit, Sequential criterion for limits, Criterion for non-existence of limit.[1] Chapter 4 (Section 4.1)

Week 2: Algebra of limits of functions with illustrations and examples, Squeeze theorem.[1] Chapter 4 (Section 4.2)

Week 3: Definition and illustration of the concepts of one-sided limits, Infinite limits and limits at infinity.
[1] Chapter 4 (Section 4.3)

Weeks 4 and 5: Definitions of continuity at a point and on a set, Sequential criterion for continuity, Algebra of continuous functions, Composition of continuous functions.
[1] Chapter 5 (Sections 5.1, and 5.2)

Weeks 6 and 7: Various properties of continuous functions defined on an interval, viz., Boundedness theorem, Maximum-minimum theorem, Statement of the location of roots theorem, Intermediate value theorem and the preservation of intervals theorem.
[1] Chapter 5 (Section 5.3)

Week 8: Definition of uniform continuity, Illustration of non-uniform continuity criteria, Uniform continuity theorem.
[1] Chapter 5 [Section 5.4 (5.4.1 to 5.4.3)]

Weeks 9 and 10: Differentiability of a function, Algebra of differentiable functions, Carathéodory's theorem and chain rule.
[1] Chapter 6 [Section 6.1 (6.1.1 to 6.1.7)]

Weeks 11 and 12: Relative extrema, Interior extremum theorem, Mean value theorem and its applications, Intermediate value property of derivatives- Darboux's theorem.
[1] Chapter 6 (Section 6.2)

Weeks 13 and 14: Taylor polynomial, Taylor's theorem and its applications, Taylor's series expansions of e^x , $\sin x$ and $\cos x$.
[1] Chapter 6 (Sections 6.4.1 to 6.4.6), and Chapter 9 (Example 9.4.14, page 286)

Subject Code	MT203	Credit: 6 (L-T-P : 5-1-0)
Subject Name	Group Theory-I	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Groups and its Elementary Properties

(Lectures: 10)

Symmetries of a square, The Dihedral groups, Definition and examples of groups including permutation groups and quaternion groups (illustration through matrices), Elementary properties of groups.

Unit 2: Subgroups and Cyclic Groups

(Lectures: 15)

Subgroups and examples of subgroups, Centralizer, Normalizer, Center of a group, Product of two subgroups; Properties of cyclic groups, Classification of subgroups of cyclic groups.

Unit 3: Permutation Groups and Lagrange's Theorem

(Lectures: 25)

Cycle notation for permutations, Properties of permutations, Even and odd permutations, alternating groups; Properties of cosets, Lagrange's theorem and consequences including Fermat's Little theorem; Normal subgroups, factor (quotient) groups, Cauchy's theorem for finite abelian groups.

Unit 4: Group Homomorphisms

(Lectures: 20)

Group homomorphisms, Properties of homomorphisms, Group isomorphisms, Cayley's theorem, Properties of isomorphisms, First, Second and Third isomorphism theorems for groups.

Reference:

1. Gallian, Joseph. A. (2013). *Contemporary Abstract Algebra* (8th ed.). Cengage Learning India Private Limited, Delhi. Fourth impression, 2015.

Additional Reading:

1. Rotman, Joseph J. (1995). *An Introduction to The Theory of Groups* (4th ed.). Springer Verlag, New York.

Teaching Plan (MT203: Group Theory-I):

Week 1: Symmetries of a square, The Dihedral groups, Definition and examples of groups including permutation groups and quaternion groups (illustration through matrices)

[1] Chapter 1

Week 2: Definition and examples of groups, Elementary properties of groups.

[1] Chapter 2

Week 3: Subgroups and examples of subgroups, Centralizer, Normalizer, Center of a Group, Product of two subgroups.

[1] Chapter 3

Weeks 4 and 5: Properties of cyclic groups. Classification of subgroups of cyclic groups. [1] Chapter 4

Weeks 6 and 7: Cycle notation for permutations, Properties of permutations, Even and odd permutations, Alternating group.

[1] Chapter 5 (up to page 110)

Weeks 8 and 9: Properties of cosets, Lagrange's theorem and consequences including Fermat's Little theorem.

[1] Chapter 7 (up to Example 6, page 150)

Week 10: Normal subgroups, Factor groups, Cauchy's theorem for finite abelian groups. [1] Chapters 9 (Theorem 9.1, 9.2, 9.3 and 9.5, and Examples 1 to 12)

Weeks 11 and 12: Group homomorphisms, Properties of homomorphisms, Group isomorphisms, Cayley's theorem.

[1] Chapter 10 (Theorems 10.1 and 10.2, Examples 1 to 11)

[1] Chapter 6 (Theorem 6.1, and Examples 1 to 8)

Weeks 13 and 14: Properties of isomorphisms, First, Second and Third isomorphism theorems. [1] Chapter 6 (Theorems 6.2 and 6.3, and Examples 1 to 8)

[1] Chapter 10 (Theorems 10.3, 10.4, Examples 12 to 14, and Exercises 41 and 42 for second and third isomorphism theorems for groups)

Subject Code	MT205	Credit: 6 (L-T-P : 4-0-2) 4 Lecture (per week) 4 Hours Practical (per week per student)
Subject Name	Multivariate Calculus	
Total Marks	150(Theory:70, Internal Assessment: 30, Practical: 50)	
Examination	3 Hours (Written) + 2 Hours (Practical)	

Course Contents:

Unit 1: Calculus of Functions of Several Variables (Lectures: 20)

Functions of several variables, Level curves and surfaces, Limits and continuity, Partial differentiation, Higher order partial derivative, Tangent planes, Total differential and differentiability, Chain rule, Directional derivatives, The gradient, Maximal and normal property of the gradient, Tangent planes and normal lines

Unit 2: Extrema of Functions of Two Variables and Properties of Vector Field (Lectures: 8)

Extrema of functions of two variables, Method of Lagrange multipliers, Constrained optimization problems; Definition of vector field, Divergence and curl.

Unit 3: Double and Triple Integrals (Lectures: 16)

Double integration over rectangular and nonrectangular regions, Double integrals in polar coordinates, Triple integral over a parallelepiped and solid regions, Volume by triple integrals, triple integration in cylindrical and spherical coordinates, Change of variables in double and triple integrals.

Unit 4: Green's, Stokes' and Gauss Divergence Theorem (Lectures: 12)

Line integrals, Applications of line integrals: Mass and Work, Fundamental theorem for line integrals, Conservative vector fields, Green's theorem, Area as a line integral; Surface integrals, Stokes' theorem, The Gauss divergence theorem.

References:

1. Strauss, Monty J., Bradley, Gerald L., & Smith, Karl J. (2007). *Calculus* (3rd ed.). Dorling Kindersley (India) Pvt. Ltd. (Pearson Education). Delhi. Indian Reprint 2011.
2. Marsden, J. E., Tromba, A., & Weinstein, A. (2004). *Basic Multivariable Calculus*. Springer (SIE). First Indian Reprint.

Teaching Plan (Theory of MT205: Multivariate Calculus):

Week 1: Definition of functions of several variables, Graphs of functions of two variables– Levelcurves and surfaces, Limits and continuity of functions of two variables.

[1] Chapter 11 (Sections 11.1 and 11.2)

Week 2: Partial differentiation, and partial derivative as slope and rate, Higher order partial derivatives.

Tangent planes, incremental approximation, Total differential.

[1] Chapter 11 (Sections 11.3 and 11.4)

Week 3: Differentiability, Chain rule for one parameter, Two and three independent parameters.[1] Chapter 11 (Sections 11.4 and 11.5)

Week 4: Directional derivatives, The gradient, Maximal and normal property of the gradient, Tangentplanes and normal lines.

[1] Chapter 11 (Section 11.6)

Week 5: First and second partial derivative tests for relative extrema of functions of two variables,and absolute extrema of continuous functions.

[1] Chapter 11 [Section 11.7 (up to page 605)]

Week 6: Lagrange multipliers method for optimization problems with one constraint, Definition of vector field, Divergence and curl.

[1] Chapter 11 [Section 11.8 (pages 610-614)], Chapter13 (Section 13.1)

Week 7: Double integration over rectangular and nonrectangular regions.

[1] Chapter 12 (Sections 12.1 and 12.2)

Week 8: Double integrals in polar co-ordinates, and triple integral over a parallelepiped.[1] Chapter 12 (Sections 12.3 and 12.4)

Week 9: Triple integral over solid regions, Volume by triple integrals, and triple integration incylindrical coordinates.

[1] Chapter 12 (Sections 12.4 and 12.5)

Week 10: Triple integration in spherical coordinates, Change of variables in double and triple integrals.[1] Chapter 12 (Sections 12.5 and 12.6)

Week 11: Line integrals and its properties, applications of line integrals: mass and work.[1] Chapter 13 (Section 13.2)

Week 12: Fundamental theorem for line integrals, Conservative vector fields and path independence.[1] Chapter 13 (Section 13.3)

Week 13: Green's theorem for simply connected region, Area as a line integral, Definition of surfaceintegrals

[1] Chapter 13 [Sections 13.4 (pages 712 to 716), 13.5 (pages 723 to 726)]

Week 14: Stokes' theorem and the divergence theorem.

[1] Chapter 13 [Sections 13.6 (pages 733 to 737), 13.7 (pages 742 to 745)]

Note. To improve the problem solving ability, for similar kind of examples based upon the abovecontents, the reference [2] may be consulted.

Multivariate Calculus Lab

List of practicals to be done using Mathematica / MATLAB / Maple/Maxima/Scilab, etc.

1. Let $f(x)$ be any function and L be any real number. For given a and $\varepsilon > 0$, find a $\delta > 0$ such that for all x satisfying $0 < |x - a| < \delta$, the inequality $0 < |f(x) - l| < \varepsilon$ holds.

For example:

(a) $f(x) = x + 1, L = 5, a = 4, \varepsilon = 0.01$

(b) $f(x) = \sqrt{x+1}, L = 1, a = 4, \varepsilon = 0.1$

(c) $f(x) = x^2, L = 4, a = -2, \varepsilon = 0.5$

(d) $f(x) = \frac{1}{x}, L = -1, a = -1, \varepsilon = 0.1$

2. Discuss the limit of the following functions when x tends to 0:

$$\pm \frac{1}{x}, \sin\left(\frac{1}{x}\right), \cos\left(\frac{1}{x}\right), x \sin\left(\frac{1}{x}\right), x \cos\left(\frac{1}{x}\right), x^2 \sin\left(\frac{1}{x}\right),$$

$$\frac{1}{x^n} (n \in \mathbb{N}), [x] \text{ greatest integer function, } \frac{1}{x} \sin(x).$$

3. Discuss the limit of the following functions when x tends to infinity:

$$e^{\pm \frac{1}{x}}, \sin\left(\frac{1}{x}\right), \frac{1}{x} e^{\pm x}, \frac{x}{x+1}, x^2 \sin\left(\frac{1}{x}\right), \frac{ax+b}{cx^2+dx+e} (a \neq 0 \neq c)$$

4. Discuss the continuity of the functions at $x = 0$ in the Practical 2.
5. Illustrate the geometric meaning of Rolle's theorem of the following functions on the given interval: (i) $x^3 - 4x$ on $[-2, 2]$; (ii) $(x-3)^2(x-5)^3$ on $[3, 5]$ etc.
6. Illustrate the geometric meaning of Lagrange's mean value theorem of the following functions on the given interval:
(i) $\log x$ on $[1/2, 2]$; (ii) $x(x-1)(x-2)$ on $[0, 1/2]$; (iii) $2x^2 - 7x + 10$ on $[2, 5]$ etc.
7. Visualization by creating graphs: Taylor's polynomials – approximated up to certain degrees.
8. Draw the following surfaces and find level curves at the given heights:
(a) $f(x, y) = 10 - x^2 - y^2; z = 1, z = 6, z = 9$
(b) $f(x, y) = x^2 + y^2; z = 1, z = 6, z = 9$
(c) $f(x, y) = x^3 - y; z = 1, z = 6$
(d) $f(x, y) = x^2 + \frac{y^2}{4}; z = 1, z = 5, z = 8$
(e) $f(x, y) = 4x^2 + y^2; z = 0, z = 1, z = 9$

9. Draw the following surfaces and discuss whether limit exists or not as (x, y) approaches to the given points. Find the limit, if it exists:
- $f(x, y) = \frac{x+y}{x-y}; (x, y) \rightarrow (0, 0)$ and $(x, y) \rightarrow (1, 3)$
 - $f(x, y) = \frac{x-y}{\sqrt{x^2+y^2}}; (x, y) \rightarrow (0, 0)$ and $(x, y) \rightarrow (2, 1)$
 - $f(x, y) = (x+y)e^{xy}; (x, y) \rightarrow (1, 1)$ and $(x, y) \rightarrow (1, 0)$
 - $f(x, y) = e^{xy}; (x, y) \rightarrow (0, 0)$ and $(x, y) \rightarrow (1, 0)$
 - $f(x, y) = \frac{x+y^2}{x^2+y^2}; (x, y) \rightarrow (0, 0)$
 - $f(x, y) = \frac{x^2-y^2}{x^2+y^2}; (x, y) \rightarrow (0, 0)$ and $(x, y) \rightarrow (2, 1)$
10. Draw the tangent plane to the following surfaces at the given point:
- $f(x, y) = \sqrt{x^2+y^2}$ at $(3, 1, \sqrt{10})$
 - $f(x, y) = 10 - x^2 - y^2$ at $(2, 2, 2)$
 - $x^2 + y^2 + z^2 = 9$ at $(3, 0, 0)$
 - $z = \tan^{-1} x$ at $(1, \sqrt{3}, \pi/3)$ and $(2, 2, \pi/4)$
 - $z = \log|x+y^2|$ at $(-3, -2, 0)$
11. Use an incremental approximation to estimate the following functions at the given point and compare it with calculated value:
- $f(x, y) = 3x^4 + 2y^4$ at $(1.01, 2.03)$
 - $f(x, y) = x^5 - 2y^3$ at $(0.98, 1.03)$
 - $f(x, y) = e^{xy}$ at $(1.01, 0.98)$
12. Find critical points and identify relative maxima, relative minima or saddle points to the following surfaces, if it exists:
- $z = x^2 + y^2;$
 - $z = 1 - x^2 - y^2;$
 - $z = y^2 - x^2$
 - $z = x^2 y^4$
13. Draw the following regions D and check whether these regions are of **Type I** or **Type II**:
- $D = \{(x, y) : 0 \leq x \leq 2, 1 \leq y \leq e^x\}$
 - $D = \{(x, y) : \log y \leq x \leq 2, 1 \leq y \leq e^2\}$
 - $D = \{(x, y) : 0 \leq x \leq 1, x^3 \leq y \leq 1\}$
 - The region D is bounded by $y = x^2 - 2$ and the line $y = x$.
 - $D = \{(x, y) : 0 \leq x \leq \frac{\pi}{4}, \sin x \leq y \leq \cos x\}$

Skill Enhancement Paper

Subject Code	MT207	Credit: 4 (L-T-P : 2-0-2) 2 Lecture (per week) 4 Hours Practical (per week per student)
Subject Name	Latex and HTML	
Total Marks	100 (Theory:35, Internal Assessment: 15, Practical: 50)	
Examination	2 Hours (Written) + 2 Hours (Practical)	

Unit 1: Getting Started with LaTeX

(Lectures: 6)

Introduction to TeX and LaTeX, Typesetting a simple document, Adding basic information to a document, Environments, Footnotes, Sectioning and displayed material.

Unit 2: Mathematical Typesetting with LaTeX

(Lectures: 6)

Accents and symbols, Mathematical Typesetting (Elementary and Advanced): Subscript/ Superscript, Fractions, Roots, Ellipsis, Mathematical Symbols, Arrays, Delimiters, Multiline formulas, Spacing and changing style in math mode.

Unit 3: Graphics and Beamer Presentation in LaTeX

(Lectures: 8)

Graphics in LaTeX, Simple pictures using PS Tricks, Plotting of functions, Beamer presentation.

Unit 4: HTML

(Lectures: 8)

HTML basics, Creating simple web pages, Images and links, Design of web pages.

References:

1. Bindner, Donald & Erickson, Martin. (2011). *A Student's Guide to the Study, Practice, and Tools of Modern Mathematics*. CRC Press, Taylor & Francis Group, LLC.
2. Lamport, Leslie (1994). *LaTeX: A Document Preparation System, User's Guide and Reference Manual* (2nd ed.). Pearson Education. Indian Reprint.

Practical/Lab work to be performed in Computer Lab.

Practicals:

- [1] Chapter 9 (Exercises 4 to 10), Chapter 10 (Exercises 1 to 4 and 6 to 9), Chapter 11 (Exercises 1, 3, 4, and 5), and Chapter 15 (Exercises 5, 6 and 8 to 11).

Teaching Plan (Theory of MT207: LaTeX and HTML):

Weeks 1 to 3: Introduction to TeX and LaTeX, Typesetting a simple document, Adding basic information to a document, Environments, Footnotes, Sectioning and displayed material.

[1] Chapter 9 (9.1 to 9.5)

[2] Chapter 2 (2.1 to 2.5)

Weeks 4 to 6: Accents of symbols, Mathematical typesetting (elementary and advanced): subscript/superscript, Fractions, Roots, Ellipsis, Mathematical symbols, Arrays, Delimiters, Multiline formulas, Spacing and changing style in math mode.

[1] Chapter 9 (9.6 and 9.7)

[2] Chapter 3 (3.1 to 3.3)

Weeks 7 and 8: Graphics in LaTeX, Simple pictures using PS Tricks, Plotting of functions.

[1] Chapter 9 (Section 9.8)

[1] Chapter 10 (10.1 to 10.3)

[2] Chapter 7 (7.1 and 7.2)

Weeks 9 and 10: Beamer presentation.

[1] Chapter 11 (Sections 11.1 to 11.4)

Weeks 11 and 12: HTML basics, Creating simple web pages.

[1] Chapter 15 (Sections 15.1 and 15.2)

Weeks 13 and 14: Adding images and links, Design of web pages.

[1] Chapter 15 (Sections 15.3 to 15.5)

Semester IV

Subject Code	MT202	Credit: 6 (L-T-P : 4-0-2) 4 Lecture (per week) 4 Hours Practical (per week per student)
Subject Name	Partial Differential Equations	
Total Marks	150 (Theory:70, Internal Assessment: 30, Practical: 50)	
Examination	3 Hours (Written) + 2 Hours (Practical)	

Unit 1: First Order PDE and Method of Characteristics (Lectures: 12)

Introduction, Classification, Construction and geometrical interpretation of first order partial differential equations (PDE), Method of characteristic and general solution of first order PDE, Canonical form of first order PDE, Method of separation of variables for first order PDE.

Unit 2: Mathematical Models and Classification of 2nd Order Linear PDE (Lectures: 12)

Gravitational potential, Conservation laws and Burger's equations, Classification of second order PDE, Reduction to canonical forms, Equations with constant coefficients, General solution.

Unit 3: The Cauchy Problem and Wave Equations (Lectures: 16)

Mathematical modeling of vibrating string, vibrating membrane. Cauchy problem for second order PDE, Homogeneous wave equation, Initial boundary value problems, Non-homogeneous boundary conditions, Finite strings with fixed ends, Non-homogeneous wave equation, Goursat problem.

Unit 4: Method of Separation of Variables (Lectures: 16)

Method of separation of variables for second order PDE, Vibrating string problem, Existence and uniqueness of solution of vibrating string problem, Heat conduction problem, Existence and uniqueness of solution of heat conduction problem, Non-homogeneous problem.

Reference:

1. Yehuda Pinchover and Jacob Rubinstein: *An introduction to Partial Differential Equations* Cambridge University Press, 2005
2. Myint-U, Tyn & Debnath, Lokenath. (2007). *Linear Partial Differential Equations for Scientist and Engineers* (4th ed.) Springer, Third Indian Reprint, 2013.

Additional Readings:

1. Sneddon, I. N. (2006). *Elements of Partial Differential Equations*, Dover Publications. Indian Reprint.

Teaching Plan (Theory of MT202: Partial Differential Equations):

Week 1: Introduction, Classification, Construction of first order partial differential equations (PDE).[1] Chapter 1 (Sections 1.2 to 1.4)

Week 2: Method of characteristics and general solution of first order PDE.
[1] Chapter 2 (Sections 2.1 and 2.4)

Week 3: Canonical form of first order PDE, Method of separation of variables for first order PDE.[2] Chapter 2 (Sections 2.6 and 2.7)

Week 4: The vibrating string, Vibrating membrane, Gravitational potential, Conservation laws.[2] Chapter 3 (Sections 3.1 to 3.3, 3.5, and 3.6)

Weeks 5 and 6: Reduction to canonical forms, Equations with constant coefficients, General solution.[1] Chapter 3 (Sections 3.1 to 3.5)

Weeks 7 and 8: The Cauchy problem for second order PDE, Homogeneous wave equation.[1] Chapter 4 (Sections 4.1 to 4.4)

Weeks 9 and 10: Initial boundary value problem, Non-homogeneous boundary conditions, Finitestring with fixed ends, Non – homogeneous wave equation, Goursat problem.
[2] Chapter 5 (Sections 5.5 to 5.7, and 5.9)

Weeks 11 and 12: Method of separation of variables for second order PDE, Vibrating string problem.[1] Chapter 5 (Sections 5.1 to 5.4)

Weeks 13 and 14: Existence (omit proof) and uniqueness of vibrating string problem. Heat conduction problem. Existence (omit proof) and uniqueness of the solution of heat conduction problem. Non – homogeneous problem.
[1] Chapter 7 (Sections 7.4 to 7.6, and 7.8)

PDE Lab

Practical /Lab work to be performed in a Computer Lab:

Modeling of the following problems using Mathematica /MATLAB/ Maple/ Maxima/ Scilab etc.

1. Solution of Cauchy problem for first order PDE.
2. Plotting the characteristics for the first order PDE.
3. Plot the integral surfaces of a given first order PDE with initial data.

4. Solution of wave equation $\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2}$ for any two of the following associated conditions:

- (a) $u(x, 0) = \phi(x), u_t(x, 0) = \psi(x), x \in \square, t > 0$
- (b) $u(x, 0) = \phi(x), u_t(x, 0) = \psi(x), u(0, t) = 0, x > 0, t > 0$
- (c) $u(x, 0) = \phi(x), u_t(x, 0) = \psi(x), u_x(0, t) = 0, x > 0, t > 0$
- (d) $u(x, 0) = \phi(x), u_t(x, 0) = \psi(x), u(0, t) = 0, u(l, t) = 0, 0 < x < l, t > 0$

5. Solution of one-Dimensional heat equation $u_t = k u_{xx}$, for a homogeneous rod of length l . That is - solve the IBVP:

$$\begin{aligned}u_t &= k u_{xx}, & 0 < x < l, & & t > 0 \\u(0, t) &= 0, & u(l, t) &= 0, & t \geq 0 \\u(0, t) &= f(x), & 0 \leq x \leq l & & \end{aligned}$$

6. Solving systems of ordinary differential equations.
7. Draw the following sequence of functions on the given interval and discuss the pointwise convergence:

- | | |
|--|---|
| (i) $f_n(x) = x^n$ for $x \in \square$ | (ii) $f_n(x) = \frac{x}{n}$ for $x \in \square$ |
| (iii) $f_n(x) = \frac{x^2 + nx}{n}$ for $x \in \square$ | (iv) $f_n(x) = \frac{\sin nx + n}{n}$ for $x \in \square$ |
| (v) $f_n(x) = \frac{x}{x+n}$ for $x \in \square, x \geq 0$ | (vi) $f_n(x) = \frac{nx}{1+n^2x^2}$ for $x \in \square$ |
| (vii) $f_n(x) = \frac{nx}{1+nx}$ for $x \in \square, x \geq 0$ | (viii) $f_n(x) = \frac{x^n}{1+x^n}$ for $x \in \square, x \geq 0$ |

8. Discuss the uniform convergence of sequence of functions (i) to (viii) given above in (7).

Subject Code	MT204	Credit: 6 (L-T-P : 5-1-0)
Subject Name	Riemann Integration and Series of Functions	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Riemann Integration

(Lectures: 25)

Definition of Riemann integration, Inequalities for upper and lower Darboux sums, Necessary and sufficient conditions for the Riemann integrability, Definition of Riemann integration by Riemann sum and equivalence of the two definitions, Riemann integrability of monotone functions and continuous functions, Properties of Riemann integrable functions, Definitions of piecewise continuous and piecewise monotone functions and their Riemann integrability, intermediate value theorem for integrals, Fundamental theorems (I and II) of calculus, and the integration by parts.

Unit 2: Improper Integral

(Lectures: 10)

Improper integrals of Type-I, Type-II and mixed type, Convergence of Beta and Gamma functions, and their properties.

Unit 3: Sequence and Series of Functions

(Lectures: 25)

Pointwise and uniform convergence of sequence of functions, Theorem on the continuity of the limit function of a sequence of functions, Theorems on the interchange of the limit and derivative, and the interchange of the limit and integrability of a sequence of functions. Pointwise and uniform convergence of series of functions, Theorems on the continuity, Derivability and integrability of the sum function of a series of functions, Cauchy criterion and the Weierstrass M-Test for uniform convergence.

Unit 4: Power Series

(Lectures: 10)

Definition of a power series, Radius of convergence, Absolute convergence (Cauchy-Hadamard theorem), Uniform convergence, Differentiation and integration of power series, Abel's Theorem.

References:

1. Bartle, Robert G., & Sherbert, Donald R. (2015). *Introduction to Real Analysis* (4th ed.). Wiley India Edition. Delhi.
2. Denlinger, Charles G. (2011). *Elements of Real Analysis*. Jones and Bartlett (Student Edition). First Indian Edition. Reprinted 2015.
3. Ghorpade, Sudhir R. & Limaye, B. V. (2006). *A Course in Calculus and Real Analysis*. Undergraduate Texts in Mathematics, Springer (SIE). First Indian reprint.
4. Ross, Kenneth A. (2013). *Elementary Analysis: The Theory of Calculus* (2nd ed.). Undergraduate Texts in Mathematics, Springer.

Teaching Plan (MT204: Riemann Integration & Series of Functions):

Week 1: Definition of Riemann integration, Inequalities for upper and lower Darboux sums.[4] Chapter 6 [Section 32 (32.1 to 32.4)]

Week 2: Necessary and sufficient conditions for the Riemann integrability, Definition of Riemann integration by Riemann sum and equivalence of the two definitions.
[4] Chapter 6 [Section 32 (32.5 to 32.10)]

Week 3: Riemann integrability of monotone functions and continuous functions, Algebra and properties of Riemann integrable functions.
[4] Chapter 6 [Section 33 (33.1 to 33.6)]

Week 4: Definitions of piecewise continuous and piecewise monotone functions and their Riemann integrability, Intermediate value theorem for integrals.
[4] Chapter 6 [Section 33 (33.7 to 33.10)]

Week 5: First and second fundamental theorems of integral calculus, and the integration by parts.[4] Chapter 6 [Section 34 (34.1 to 34.3)]

Week 6: Improper integrals of Type-I, Type-II and mixed type.
[2] Chapter 7 [Section 7.8 (7.8.1 to 7.8.18)]

Week 7: Convergence of Beta and Gamma functions, and their properties.
[3] Pages 405 - 408

Week 8: Definitions and examples of pointwise and uniformly convergent sequence of functions.[1] Chapter 8 [Section 8.1 (8.1.1 to 8.1.10)]

Week 9: Motivation for uniform convergence by giving examples. Theorem on the continuity of the limit function of a sequence of functions.
[1] Chapter 8 [Section 8.2 (8.2.1 to 8.2.2)]

Week 10: The statement of the theorem on the interchange of the limit function and derivative, and its illustration with the help of examples. The interchange of the limit function and integrability of a sequence of functions.
[1] Chapter 8 [Section 8.2 (Theorems 8.2.3, and 8.2.4)]

Week 11: Pointwise and uniform convergence of series of functions, Theorems on the continuity, derivability and integrability of the sum function of a series of functions.
[1] Chapter 9 [Section 9.4 (9.4.1 to 9.4.4)]

Week 12: Cauchy criterion for the uniform convergence of series of functions, and the Weierstrass M-Test for uniform convergence.
[2] Chapter 9 [Section 9.4 (9.4.5 to 9.4.6)]

Week 13: Definition of a power series, Radius of convergence, Absolute and uniform convergence of a power series.
[4] Chapter 4 (Section 23)

Week 14: Differentiation and integration of power series, Statement of Abel's Theorem and its illustration with the help of examples.
[4] Chapter 4 [Section 26 (26.1 to 26.6)]

Subject Code	MT206	Credit: 6 (L-T-P : 5-1-0)
Subject Name	Ring Theory and Linear Algebra-I	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Introduction of Rings

(Lectures: 20)

Definition and examples of rings, Properties of rings, Subrings, Integral domains and fields, characteristic of a ring. Ideals, Ideal generated by a subset of a ring, Factor rings, Operations on ideals, Prime and maximal ideals.

Unit 2: Ring Homomorphisms

(Lectures: 10)

Ring homomorphisms, Properties of ring homomorphisms, First, Second and Third Isomorphism theorems for rings, The Field of quotients.

Unit 3: Introduction of Vector Spaces

(Lectures: 20)

Vector spaces, Subspaces, Algebra of subspaces, Quotient spaces, Linear combination of vectors, Linear span, Linear independence, Basis and dimension, Dimension of subspaces.

Unit 4: Linear Transformations

(Lectures: 20)

Linear transformations, Null space, Range, Rank and nullity of a linear transformation, Matrix representation of a linear transformation, Algebra of linear transformations. Isomorphisms, Isomorphism theorems, Invertibility and the change of coordinate matrix.

References:

1. Gallian, Joseph. A. (2013). *Contemporary Abstract Algebra* (8th ed.). Cengage Learning India Private Limited. Delhi. Fourth impression, 2015.
2. Friedberg, Stephen H., Insel, Arnold J., & Spence, Lawrence E. (2003). *Linear Algebra* (4th ed.). Prentice-Hall of India Pvt. Ltd. New Delhi.

Teaching Plan (MT206: Ring Theory & Linear Algebra-I):

Week 1: Definition and examples of rings, Properties of rings, Subrings.
[1] Chapter 12

Week 2: Integral domains and fields, Characteristic of a ring.
[1] Chapter 13

Week 3 and 4: Ideals, Ideal generated by a subset of a ring, Factor rings, Operations on ideals, Prime and maximal ideals.
[1] Chapter 14

Week 5: Ring homomorphisms, Properties of ring homomorphisms.
[1] Chapter 15 (up to Theorem 15.2)

Week 6: First, Second and Third Isomorphism theorems for rings, The Field of quotients.
[1] Chapter 15 (Theorems 15.3 to 15.6, Examples 10 to 12), and Exercises 3 and 4 on page 347.

Week 7: Vector spaces, subspaces, Algebra of subspaces.
[2] Chapter 1 (Sections 1.2, and 1.3)

Week 8: Linear combination of vectors, Linear span, Linear independence.
[2] Chapter 1 (Sections 1.4, and 1.5)

Weeks 9 and 10: Bases and dimension. Dimension of subspaces.
[2] Chapter 1 (Section 1.6)

Week 11: Linear transformations, Null space, Range, Rank and nullity of a linear transformation.[2] Chapter 2 (Section 2.1)

Weeks 12 and 13: Matrix representation of a linear transformation, Algebra of linear transformations.[2] Chapter 2 (Sections 2.2, and 2.3)

Week 14: Isomorphisms, Isomorphism theorems, Invertibility and the change of coordinate matrix.[2] Chapter 2 (Sections 2.4, and 2.5)

Skill Enhancement Paper

Subject Code	MT208	Credit: 4 (L-T-P : 2-0-2) 2 Lecture (per week) 4 Hours Practical (per week per student)
Subject Name	Computer Algebra Systems and Related Software	
Total Marks	100 (Theory:35, Internal Assessment: 15, Practical: 50)	
Examination	2 Hours (Written) + 2 Hours (Practical)	

Unit 1: Introduction to CAS and Applications

(Lectures: 10)

Computer Algebra System (CAS), Use of a CAS as a calculator, Computing and plotting functions in 2D, Plotting functions of two variables using Plot3D and ContourPlot, Plotting parametric curves surfaces, Customizing plots, Animating plots, Producing tables of values, working with piecewise defined functions, Combining graphics.

Unit 2: Working with Matrices

(Lectures: 6)

Simple programming in a CAS, Working with matrices, Performing Gauss elimination, operations (transpose, determinant, inverse), Minors and cofactors, Working with large matrices, Solving system of linear equations, Rank and nullity of a matrix, Eigenvalue, eigenvector and diagonalization.

Unit 3: R - The Statistical Programming Language

(Lectures: 6)

R as a calculator, Explore data and relationships in R. Reading and getting data into R: Combine and scan commands, Types and structure of data items with their properties. Manipulating vectors, Data frames, Matrices and lists. Viewing objects within objects. Constructing data objects and conversions.

Unit 4: Data Analysis with R

(Lectures: 6)

Summary commands: Summary statistics for vectors, Data frames, Matrices and lists. Summary tables. Stem and leaf plot, Histograms. Plotting in R: Box-whisker plots, Scatter plots, Pairs plots, Line charts, Pie charts, Cleveland dot charts and bar charts. Copy and save graphics to other applications.

References:

1. Bindner, Donald & Erickson, Martin. (2011). *A Student's Guide to the Study, Practice, and Tools of Modern Mathematics*. CRC Press, Taylor & Francis Group, LLC.
2. Ian Thompson, *Understanding Maple*, Cambridge University Press.
3. Gardener, M. (2012). *Beginning R: The Statistical Programming Language*, Wiley.

Note: Theoretical and Practical demonstration should be carried out only in **one** of the CAS: MAPLE/Scilab or any other.

Practical/Lab work to be performed in Computer Lab.

Practicals:

[1] Chapter 12 (Exercises 1 to 4 and 8 to 12), Chapter 14 (Exercises 1 to 3)

[2] Cover most of the content from this.

Note: Relevant exercises of [3] Chapters 2 to 5 and 7 (The practical may be done on the database to be downloaded from <http://data.gov.in/>).

Teaching Plan (MT208: Computer Algebra Systems and Related Software):

Weeks 1 to 3: Computer Algebra System (CAS), Use of a CAS as a calculator, Computing and plotting functions in 2D, producing tables of values, working with piecewise defined functions, Combining graphics. Simple programming in a CAS.

[1] Chapter 12 (Sections 12.1 to 12.5)

[2] Chapter 1, and Chapter 3 (Sections 3.1 to 3.6, and 3.8)

Weeks 4 and 5: Plotting functions of two variables using Plot3D and ContourPlot, Plotting parametric curves surfaces, Customizing plots, Animating plots.

[2] Chapter 6 (Sections 6.2, and 6.3)

Weeks 6 to 8: Working with matrices, Performing Gauss elimination, operations (Transpose, Determinant, Inverse), Minors and cofactors, working with large matrices, Solving system of linear equations, Rank and nullity of a matrix, Eigenvalue, Eigenvector and diagonalization.

[2] Chapter 7 (Sections 7.1 to 7.8)

Weeks 9 to 11: **R** as a calculator, explore data and relationships in **R**. Reading and getting data into **R**: Combine and scan commands, Types and structure of data items with their properties. Manipulating vectors, Data frames, Matrices and Lists. Viewing objects within objects. Constructing data objects and conversions.

[1] Chapter 14 (Sections 14.1 to 14.4)

[3] Chapter 2, and Chapter 3

Weeks 12 to 14: Summary commands: Summary statistics for vectors, Data frames, Matrices and lists. Summary tables. Stem and leaf plot, histograms. Plotting in **R**: Box-whisker plots, Scatter plots, Pairs plots, Line charts, Pie charts, Cleveland dot charts and Bar charts. Copy and save graphics to other applications.

[1] Chapter 14 (Section 14.7)

[3] Chapter 5 (up to page 157), and Chapter 7.

Semester V

Subject Code	MT301	Credit: 6 (L-T-P : 5-1-0)
Subject Name	Metric Spaces	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Basic Concepts

(Lectures: 15)

Metric spaces: Definition and examples, Sequences in metric spaces, Cauchy sequences, Complete metric space.

Unit 2: Topology of Metric Spaces

(Lectures: 25)

Open and closed ball, Neighborhood, Open set, Interior of a set, limit point of a set, derived set, closed set, closure of a set, diameter of a set, Cantor's theorem, Subspaces, Dense set.

Unit 3: Continuity & Uniform Continuity in Metric Spaces

(Lectures: 15)

Continuous mappings, Sequential criterion and other characterizations of continuity, Uniform continuity, Homeomorphism, Contraction mapping, Banach fixed point theorem.

Unit 4: Connectedness and Compactness (Lectures: 15)

Connectedness, Connected subsets of \mathbb{R}^n , Connectedness and continuous mappings, Compactness, Compactness and boundedness, Continuous functions on compact spaces.

Reference:

1. Shirali, Satish & Vasudeva, H. L. (2009). *Metric Spaces*, Springer, First Indian Print.

Additional Readings:

1. Kumaresan, S. (2014). *Topology of Metric Spaces* (2nd ed.). Narosa Publishing House. New Delhi.
2. Simmons, G. F. (2004). *Introduction to Topology and Modern Analysis*. Tata McGraw Hill. New Delhi.

Teaching Plan (MT301: Metric Spaces):

Week 1: Definition of metric space, Illustration using the usual metric on \mathbb{R} , Euclidean and max metric on \mathbb{R}^2 , Euclidean and max metric on \mathbb{R}^n , Discrete metric, Sup metric on $B(S)$ and $C[a, b]$, Integral metric on $C[a, b]$ etc.

[1] Chapter 1 [Section 1.2 (1.2.1, 1.2.2 ((i), (ii), (iv), (v), (viii), (ix), (x)), 1.2.3, and 1.2.4 (i))]

Week 2: Sequences in metric space, Definition of limit of a sequence, Illustration through examples, Cauchy sequences.

[1] Chapter 1 [Section 1.3 (1.3.1, 1.3.2, 1.3.3 ((i), (iv)), 1.3.5), Section 1.4 (1.4.1 to 1.4.4)]

Week 3: Definition of complete metric spaces, Illustration through examples.

[1] Chapter 1 [Section 1.4 (1.4.5 to 1.4.7, 1.4.12 to 1.4.14(ii))]

Week 4: Open and closed balls, Neighborhood, Open sets, Examples and basic results. [1] Chapter 2 [Section 2.1 (2.1.1 to 2.1.11 (except 2.1.6(ii)))]

Week 5: Interior point, Interior of a set, Limit point, Derived set, Examples and basic results. [1] Chapter 2 [Section 2.1 (2.1.12 to 2.1.20)]

Week 6: Closed set, Closure of a set, Examples and basic results.

[1] Chapter 2 [Section 2.1 (2.1.21 to 2.1.35)]

Week 7: Bounded set, Diameter of a set, Cantor's theorem.

[1] Chapter 2 [Section 2.1 (2.1.41 to 2.1.44)]

Week 8: Relativisation and subspaces, Dense sets.

[1] Chapter 2 [Section 2.2 (2.2.1 to 2.2.6), Section 2.3 (2.3.12 to 2.3.13(iv))]

Weeks 9 to 11: Continuous mappings, Sequential and other characterizations of continuity, Uniform continuity, Homeomorphism, Contraction mappings, Banach fixed point theorem.

[1] Chapter 3 [Section 3.1, Section 3.4 (3.4.1 to 3.4.8), Section 3.5 (3.5.1 to 3.5.7(iii)), and Section 3.7 (3.7.1 to 3.7.5)]

Weeks 12 to 14: Connectedness and compactness, Definitions and properties of connected and compact spaces.

[1] Chapter 4 [Section 4.1 (4.1.1 to 4.1.12)], and Chapter 5 [Section 5.1 (5.1.1 to 5.1.6), and Section 5.3 (5.3.1 to 5.3.10)]

Subject Code	MT303	Credit: 6 (L-T-P : 5-1-0)
Subject Name	Group Theory-II	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Course Objectives: The course will develop an in-depth understanding of one of the most important branch of the abstract algebra with applications to practical real-world problems. Classification of all finite Abelian groups (up to isomorphism) can be done.

Course Learning Outcomes: The course shall enable students to learn about:

- i) Automorphisms for constructing new groups from the given group.
- ii) External direct product $Z_2 \oplus Z_2$ applies to data security and electric circuits.
- iii) Group actions, Sylow theorems and their applications to check no simplicity.

Course Contents:

Unit 1: Automorphisms and Properties (Lectures: 10)

Automorphism, inner automorphism, Automorphism groups, Automorphism groups of finite and infinite cyclic groups, Characteristic subgroups, Commutator subgroup and its properties; Applications of factor groups to automorphism groups.

Unit 2: External and Internal Direct Products of Groups (Lectures: 15)

External direct products of groups and its properties, The group of units modulo n as an external direct product, Applications to data security and electric circuits; Internal direct products, Classification of groups of order p^2 , where p is a prime; Fundamental theorem of finite Abelian groups and its isomorphism classes.

Unit 3: Group Action (Lectures: 20)

Group actions and permutation representations; Stabilizers and kernels of group actions; Groups acting on themselves by left multiplication and consequences; Conjugacy in S_n .

Unit 4: Sylow Theorems and Applications (Lectures: 25)

Conjugacy classes, The class equation, p -groups, The Sylow theorems and consequences, Applications of Sylow theorems; Finite simple groups, Nonsimplicity tests; Generalized Cayley's theorem, Index theorem, Embedding theorem and applications. Simplicity of A_5 .

References:

1. Dummit, David S., & Foote, Richard M. (2016). *Abstract Algebra* (3rd ed.). Student Edition. Wiley India.
2. Gallian, Joseph. A. (2013). *Contemporary Abstract Algebra* (8th ed.). Cengage Learning India Private Limited. Delhi. Fourth impression, 2015.

Teaching Plan (MT303: Group Theory-II):

Week 1: Automorphism, Inner automorphism, Automorphism groups, Automorphism groups of finite and infinite cyclic groups.

[2] Chapter 6 (pages 135 to 138)

Week 2: Characteristic subgroups, Commutator subgroup and its properties; Applications of factor groups to automorphism groups.

[2] Exercises 1 to 4 on page 181, and Exercises 62, 68 on page 204.

[2] Chapter 9 (Theorem 9.4 and Example 17)

Week 3: External direct products of groups and its properties, The group of units modulo n as an external direct product, Applications to data security and electric circuits.

[2] Chapter 8

Week 4: Internal direct products, Classification of groups of order p^2 , where p is a prime.

[2] Chapter 9 (Section on internal direct products, pages 195 to 200)

Week 5: Statement of the Fundamental theorem of finite Abelian groups, The isomorphism classes of Abelian groups.

[2] Chapter 11

Weeks 6 and 7: Group actions and permutation representations; Stabilizers and kernels of group actions.

[1] Chapter 1 (Section 1.7), Chapter 2 (Section 2.2), and Chapter 4 (Section 4.1, except cycle decompositions)

Weeks 8 and 9: Groups acting on themselves by left multiplication and consequences; Conjugacy in S_n .

[1] Chapter 4 [Section 4.2, and Section 4.3 (Pages 125-126)]

Week 10: Conjugacy classes, The class equation, p -groups.

[2] Chapter 24 (Pages 409 to 411)

Weeks 11 and 12: State three Sylow theorems and give their applications.

[2] Chapter 24 (Pages 412 to 421)

Weeks 13 and 14: Finite simple groups, Nonsimplicity tests; Generalized Cayley's theorem, Index theorem, Embedding theorem and applications; Simplicity of A_5 .

[2] Chapter 25

Discipline Specific Elective (DSE) Course -1 (including practical)

Any *one* of the following:

MT305	Numerical Analysis
MT307	Mathematical Modelling and Graph Theory
MT309	C++ Programming for Mathematics

MT305:Numerical Analysis

Subject Code	MT305	Credit: 6 (L-T-P : 4-0-2) 4 Lecture (per week) 4 Hours Practical (per week per student)
Subject Name	Numerical Analysis	
Total Marks	150 (Theory:70, Internal Assessment: 30, Practical: 50)	
Examination	3 Hours (Written) + 2 Hours (Practical)	

Unit 1: Methods for Solving Algebraic and Transcendental Equations (Lectures: 16)
Algorithms, Convergence, Bisection method, False position method, Fixed point iteration method, Newton's method, Secant method

Unit 2: Techniques to Solve Linear Systems (Lectures: 12)
Partial and scaled partial pivoting, LU decomposition and its applications, Iterative methods: Gauss-Jacobi, Gauss-Seidel and SOR methods.

Unit 3: Interpolation (Lectures: 12)
Lagrange and Newton interpolation, Piecewise linear interpolation.

Unit 4: Numerical Differentiation and Integration (Lectures: 16)
First order and higher order approximation for first derivative, Approximation for second derivative. Numerical integration by closed Newton-Cotes formula: trapezoidal rule, Simpson's rule and its error analysis. Euler's method to solve ODE's.

Note: Emphasis is to be laid on the algorithms of the above numerical methods.

Reference:

1. Bradie, Brian. (2006). *A Friendly Introduction to Numerical Analysis*. Pearson Education, India. Dorling Kindersley (India) Pvt. Ltd. Third impression 2011.

Additional Readings:

1. Jain, M. K., Iyengar, S. R. K., & Jain, R. K. (2012). *Numerical Methods for Scientific and Engineering Computation*. (6th ed.). New Age International Publisher, India, 2016.
2. Gerald, C. F., & Wheatley, P. O. (2008). *Applied Numerical Analysis* (7th ed.). Pearson Education. India.

Numerical Analysis Lab

Practical/Lab work to be performed in Computer Lab:

Use of computer algebra software (CAS), for example Mathematica/MATLAB/Maple/Maxima/Scilab etc., for developing the following numerical programs:

- (1) Bisection method
- (2) Newton Raphson method
- (3) Secant method
- (4) Regula Falsi method
- (5) LU decomposition method
- (6) Gauss-Jacobi method
- (7) SOR method
- (8) Gauss-Seidel method
- (9) Lagrange interpolation
- (10) Newton interpolation
- (11) Trapezoidal rule
- (12) Simpson's rule
- (13) Euler's method

Note: For any of the CAS: Maple/MATLAB/Scilab etc., data types-simple data types, floating data types, character data types, arithmetic operators and operator precedence, variables and constant declarations, expressions, input/output, relational operators, logical operators and logical expressions, control statements and loop statements, Arrays should be introduced to the students.

Teaching Plan (Theory of MT305 Numerical Analysis):

Week 1: Algorithms, Convergence, Order of convergence and examples.

[1] Chapter 1 (Sections 1.1, and 1.2)

Week 2: Bisection method, False position method and their convergence analysis, Stopping condition and algorithms.

[1] Chapter 2 (Sections 2.1, and 2.2)

Week 3: Fixed point iteration method, its order of convergence and stopping condition. [1] Chapter 2 (Section 2.3)

Week 4: Newton's method, Secant method, their order of convergence and convergence analysis. [1] Chapter 2 (Sections 2.4, and 2.5)

Week 5: Examples to understand partial and scaled partial pivoting. LU decomposition. [1] Chapter 3 (Sections 3.2, and 3.5, up to Example 3.15)

Weeks 6 and 7: Application of LU decomposition to solve system of linear equations. Gauss-Jacobimethod, Gauss-Seidel and SOR iterative methods to solve system of linear equations.

[1] Chapter 3 (Sections 3.5, and 3.8)

Week 8: Lagrange interpolation: Linear and higher order interpolation, and error in it. [1] Chapter 5 (Section 5.1)

Weeks 9 and 10: Divided difference and Newton interpolation. Piecewise linear interpolation. [1] Chapter 5 (Sections 5.3, and 5.5)

Weeks 11 and 12: First order and higher order approximation for first derivative and error in the approximation. Second order forward, Backward and central difference approximations for second derivative.

[1] Chapter 6 (Section 6.2)

Week 13: Numerical integration: Trapezoidal rule, Simpson's rule and its error analysis. [1] Chapter 6 (Section 6.4)

Week 14: Euler's method to solve first order ODE initial value problems.

[1] Chapter 7 (Section 7.2 up to page 562)

MT307: Mathematical Modelling and Graph Theory

Subject Code	MT307	Credit: 6 (L-T-P: 4-0-2) 4 Lecture (per week) 4 Hours Practical (per week per student)
Subject Name	Mathematical Modelling and Graph Theory	
Total Marks	150 (Theory:70, Internal Assessment: 30, Practical: 50)	
Examination	3 Hours (Written) + 2 Hours (Practical)	

Unit 1: Power Series Solutions

(Lectures: 16)

Power series solution of a differential equation about an ordinary point, Solution about a regular singular point, The method of Frobenius. Legendre's and Bessel's equation.

Unit 2: Laplace Transforms

(Lectures: 8)

Laplace transform and inverse transform, application to initial value problem up to second order.

Unit 3: Monte Carlo Simulation

(Lectures: 16)

Monte Carlo Simulation Modeling: Simulating deterministic behavior (area under a curve, volume under a surface); Generating Random Numbers: Middle square method, Linear congruence; Queuing Models: Harbor system, Morning rush hour. Overview of optimization modeling; Linear Programming Model: Geometric solution, Algebraic solution, Simplex method, Sensitivity analysis.

Unit 4: Graph Theory

(Lectures: 16)

Graphs, Diagraphs, Networks and subgraphs, Vertex degree, Paths and cycles, Regular and bipartite graphs, Four cube problem, Social networks, Exploring and traveling, Eulerian and Hamiltonian graphs, Applications to dominoes, Diagram tracing puzzles, Knight's tour problem, Gray codes.

References:

1. Aldous, Joan M., & Wilson, Robin J. (2007). *Graphs and Applications: An Introductory Approach*. Springer. Indian Reprint.
2. Edwards, C. Henry, Penney, David E., &Calvis, David T. (2015). *Differential Equation and Boundary Value Problems: Computing and Modeling* (5th ed.). Pearson.
3. Giordano, Frank R., Fox, William P., & Horton, Steven B. (2014). *A First Course in Mathematical Modeling* (5th ed.). Brooks/Cole, Cengage Learning.

Note: [1] Chapter 1 (Section 1.1), Chapter 2 (Sections 2.1 to 2.4), Chapter 3 (Sections 3.1 to 3.3) are to be reviewed only. This is in order to understand the models on Graph Theory.

Mathematical Modeling Lab

Practical / Lab work to be performed in Computer Lab:

Modeling of the following problems using Mathematica/MATLAB/Maple /Maxima/Scilab etc.

- (i). Plotting of Legendre polynomial for $n = 1$ to 5 in the interval $[0, 1]$. Verifying graphically that all the roots of $P_n(x)$ lie in the interval $[0, 1]$.
- (ii). Automatic computation of coefficients in the series solution near ordinary points.
- (iii). Plotting of the Bessel's function of first kind of order 0 to 3.
- (iv). Automating the Frobenius Series Method.
- (v). Random number generation and then use it for one of the following:
 - a) Simulate area under a curve.
 - b) Simulate volume under a surface.
- (vi). Programming of either one of the queuing model:
 - a) Single server queue (e.g. Harbor system).
 - b) Multiple server queue (e.g. Rush hour).
- (vii). Programming of the Simplex method for 2 / 3 variables.

Teaching Plan (Theory of MT307: Mathematical Modeling and Graph Theory):

Weeks 1 and 3: Power series solution of a differential equation about an ordinary point, Solution about a regular singular point. Legendre's equation. The method of Frobenius.

[2] Chapter 8 (Sections 8.1 to 8.3)

Week 4: Bessel's equation. Bessel's function of first kind. [2] Chapter 8 [Section 8.5 up to Equation (19), page 551]

Weeks 5 and 6: Laplace transform and inverse transform, Application to initial value problem up to second order.

[2] Chapter 7 (Sections 7.1 to 7.3)

Weeks 7 and 8: Monte Carlo Simulation Modeling: Simulating deterministic behavior (area under a curve, volume under a surface), Generating Random Numbers: Middle square method, Linear congruence. Queuing Models: Harbor system, Morning rush hour.

[3] Chapter 5 (Sections 5.1 to 5.2, and 5.5)

Weeks 9 and 10: Overview of optimization modeling, Linear Programming Model: Geometric solution, Algebraic solution, Simplex method, Sensitivity analysis.

[3] Chapter 7

Weeks 11 and 12: Graphs, Diagraphs, Networks and subgraphs, Vertex degree, Paths and cycles, Regular and bipartite graphs, Four cube problem, Social networks.

[1] Chapter 1 (Section 1.1), and Chapter 2

Weeks 13 and 14: Overview of optimization modeling, Linear Programming Model: Geometric solution, Algebraic solution, Simplex method, Sensitivity analysis.

[1] Chapter 3

MT309: C++ Programming for Mathematics

Subject Code	MT309	Credit: 6 (L-T-P: 4-0-2) 4 Lecture (per week) 4 Hours Practical (per week per student)
Subject Name	C++ Programming for Mathematics	
Total Marks	150 (Theory:70, Internal Assessment: 30, Practical: 50)	
Examination	3 Hours (Written) + 2 Hours (Practical)	

Unit 1: C++ Essentials

(Lectures: 16)

Fundamentals of programming, Organization of logic flow in stored program model of computation, C++ as a general purpose programming language, Structure of a C++ program, Common compilers and IDE's, Basic data-types, Variables and literals in C++, Operators, Expressions, Evaluation precedence, and Type compatibility. Outline of program development in C++, Debugging and testing. Applications: Greatest common divisor, and Random number generation.

Unit 2: Working with Structured Data

(Lectures: 12)

Structured data-types in C++, Arrays and manipulating data in arrays with applications in factorization of an integer and finding Euler's totient; Objects and classes: Information hiding, Modularity, Constructors and Destructors, Methods and Polymorphism. Applications: Cartesian geometry using points (2 & 3-dimensional), and Pythagorean triples.

Unit 3: Working with Containers and Templates

(Lectures: 16)

Containers and Template Libraries: Sets, Iterators, Multisets, Vectors, Maps, Lists, Stacks and Queues. Applications: Basic set algebra, Modulo arithmetic, Permutations, and Polynomials.

Unit 4: Using Mathematical Libraries and Packages

(Lectures: 12)

Arbitrary precision arithmetic using the GMP package; Linear algebra: Two-dimensional arrays in C++ with applications in finding Eigenvalues, Eigenvectors, Rank, Nullity, and Solving system of linear equations in matrices. Features of C++ for input/output and visualization: Strings, Streams, Formatting methods, Processing files in a batch, Command-line arguments, Visualization packages and their use in plots.

Reference:

1. Scheinerman, Edward (2006). *C++ for Mathematicians: An Introduction for Students and Professionals*. Chapman & Hall/CRC. Taylor & Francis Group, LLC.

Additional Readings:

1. Dale, Nell & Weems, Chip (2013). *Programming and Problem Solving with C++* (6th ed.). Comprehensive Edition. Jones & Bartlett Learning.
2. Gottschling, Peter (2016). *Discovering Modern C++: An Intensive Course for Scientists, Engineers, and Programmers*. Addison-Wesley. Pearson Education, Inc.
3. Josuttis, Nicolai M. (2012). *The C++ Standard Library: A Tutorial and Reference* (2nd ed.). Addison-Wesley. Pearson Education, Inc.
4. Lippman, Stanley B. (2000). *Essential C++*. Addison-Wesley.
5. Stroustrup, Bjarne (2013). *The C++ Programming Language* (4th ed.). Addison-Wesley.

C++ Programming Lab for Mathematics

Practical / Lab work to be performed in Computer Lab:

A: Preparatory (Practical Sessions: 8 Hrs.)

1. Setting up of C++ programming environment on Linux/Windows/Mac-OS; gcc/g++/mingw/cc, Program-development methodology and use IDE's or other tools.
2. Demonstration of sample programs for
 - a. "Hello World"
 - b. Sum of an arithmetic progression.
 - c. Value of $\sin x$ using series expansion.
3. Finding/demonstrating:
 - a. Machine epsilon.
 - b. Integer and float overflow/underflow.
 - c. Iteration and selection based logic.(provide a list of 8-10 problems suitable to learners needs)

B: Evaluative:

Set-I: (Practical Sessions: 8 Hrs.)

1. Greatest common divisor (including Euclid's Method).
2. Random number generation (including a Monte Carlo Program).

Set-II: (Practical Sessions: 12 Hrs.)

1. Factorization of an integer, and Euler's totient.
2. Cartesian geometry using points (2 & 3-dimensional).
3. Pythagorean triples.

Set-III: (Practical Sessions: 16 Hrs.)

1. Basic set algebra.
2. Modulo arithmetic.
3. Permutations.
4. Polynomials.

Set-IV: (Practical Sessions: 12 Hrs.)

1. Arbitrary precision arithmetic using the GMP package.
2. Finding Eigenvalues, Eigenvectors, Rank, Nullity, and Solving system of linear equations in matrices.
3. Plots (using the GNU plotutils package).

Note. Exception handling in lab-exercises (SET-I to IV), Comments/Documentation using Doxygen may be emphasized.

Teaching Plan (Theory of MT309 C++ Programming for Mathematics):

Week 1: Fundamentals of programming, Organization of logic flow in stored program model of computation, C++ as a general purpose programming language, Structure of a C++ program, Common compilers and IDE's, Basic data-types.

[1] Chapter 1, and Chapter 2 (Sections 2.1 to 2.3)

Week 2: Variables and literals in C++, Operators, Expressions, Evaluation precedence, and Type compatibility. Outline of program development in C++, Debugging and testing.

[1] Chapter 2 (Sections 2.4 to 2.9)

Weeks 3 and 4: Applications: Greatest common divisor, and Random number generation. [1] Chapter 3, and Chapter 4

Week 5: Structured data-types in C++, Arrays and manipulating data in arrays.

Applications: Factorization of an integer, and Euler's totient.

[1] Chapter 5 (Sections 5.1 to 5.4)

Weeks 6 and 7: Objects and classes: Information hiding, Modularity, Constructors and Destructors, Methods and Polymorphism. Applications: Cartesian geometry using points (two and three dimensional), and Pythagorean triples.

[1] Chapter 6, and Chapter 7

Weeks 8 and 9: Containers and Template Libraries: Sets, Iterators, Multisets, Vectors, Maps, Lists, Stacks and Queues with applications in basic set algebra.

[1] Chapter 8 [Sections 8.1 to 8.7 (8.7.1 – 8.7.3)]

Weeks 10 and 11: Applications: Modulo arithmetic, Permutations, and Polynomials.

[1] Chapter 9, Chapter 11 (Sections 11.1, and 11.2), and Chapter 12 (Sections 12.1 to 12.3)

Week 12: Arbitrary precision arithmetic using the GMP package; Linear algebra: Two-dimensional arrays in C++ with applications in finding Eigenvalues, Eigenvectors, Rank, Nullity, and Solving system of linear equations in matrices.

[1] Chapter 13 [Sections 13.1, and 13.2 (13.2.1, 13.2.2)]

Weeks 13 and 14: Features of C++ for input/output & visualization: Strings, Streams, Formatting methods, Processing files in a batch, Command-line arguments, Visualization packages and their use in plots.

[1] Chapter 14 [Sections 14.1 to 14.6, and 14.8 (14.8.1-14.8.3)]

Discipline Specific Elective (DSE) Course - 2

Any one of the following:

MT311	Probability Theory and Statistics
MT313	Discrete Mathematics
MT315	Cryptography and Network Security

MT311:Probability Theory and Statistics

Subject Code	MT311	Credit: 6 (L-T-P: 5-1-0)
Subject Name	Probability Theory and Statistics	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Probability Functions and Moment Generating Function (Lectures: 20)

Sample space, Probability set function, Real random variables - Discrete and continuous, Cumulative distribution function, Probability mass/density functions, Transformations, Mathematical expectation, Moments, Moment generating function, Characteristic function.

Unit 2: Univariate Discrete and Continuous Distributions (Lectures: 20)

Discrete distributions: Uniform, Bernoulli, Binomial, Negative binomial, Geometric and Poisson; Continuous distributions: Uniform, Gamma, Exponential, Chi-square, Beta and normal; Normal approximation to the binomial distribution.

Unit 3: Bivariate Distribution (Lectures: 10)

Joint cumulative distribution function and its properties, Joint probability density function, Marginal distributions, Expectation of function of two random variables, Joint moment generating function, Conditional distributions and expectations.

Unit 4: Correlation, Regression and Central Limit Theorem (Lectures: 20)

The Correlation coefficient, Covariance, Calculation of covariance from joint moment generating function, Independent random variables, Linear regression for two variables, The method of least squares, Bivariate normal distribution, Chebyshev's theorem, Strong law of large numbers, Central limit theorem and weak law of large numbers.

References:

1. Hogg, Robert V., McKean, Joseph W., & Craig, Allen T. (2013). *Introduction to Mathematical Statistics* (7th ed.). Pearson Education, Inc.
2. Miller, Irwin & Miller, Marylees. (2014). John E. Freund's *Mathematical Statistics with Applications* (8th ed.). Pearson. Dorling Kindersley (India).
3. Ross, Sheldon M. (2014). *Introduction to Probability Models* (11th ed.). Elsevier Inc. AP.

Teaching Plan (MT311: Probability Theory and Statistics):

Weeks 1 and 2: Sample space, Probability set function and examples, Random variable, Probability mass/density function, Cumulative distribution function and its properties.

[1] Chapter 1 (Sections 1.1, 1.3, and 1.5)

Week 3: Discrete and continuous random variables, and Transformations.

[1] Chapter 1 (Sections 1.6, and 1.7)

Week 4: Expectation of random variables, and some special expectations: Mean, Variance, Standard deviation, Moments and moment generating function, Characteristic function.

[1] Chapter 1 (Sections 1.8, and 1.9)

Week 5: The discrete distributions - Uniform, Bernoulli and binomial.

[2] Chapter 5 (Sections 5.2 to 5.4)

Week 6: The discrete distributions - negative Binomial, Geometric and Poisson.

[2] Chapter 5 (Sections 5.5, and 5.7)

Week 7: The continuous distributions - Uniform, Gamma, Exponential, Chi-square and Beta. [2] Chapter 6 (Sections 6.2 to 6.4)

Week 8: Normal distribution, and normal approximation to the binomial distribution. [2] Chapter 6 (Sections 6.5, and 6.6)

Weeks 9 and 10: Random vector: Discrete and continuous, Joint cumulative distribution function and its properties, Joint probability mass/density function, Marginal probability mass function, and expectation of two random variables, Joint moment generating function, Conditional distributions and expectations.

[1] Chapter 2 (Sections 2.1, and 2.3)

Week 11: The Correlation coefficient, Covariance, Calculation of covariance from joint moment generating function, Independent random variables.

[1] Chapter 2 (Section 2.4, and Section 2.5)

Week 12: Linear regression for two variables, and the method of least squares.

[2] Chapter 14 (Sections 14.1 to 14.3)

Week 13: Bivariate normal distribution; Chebyshev's theorem.

[2] Chapter 6 (Section 6.7), and Chapter 4 (Section 4.4)

Week 14: Statement and interpretation of the strong law of large numbers, Central limit theorem and the weak law of large numbers.

[3] Chapter 2 (Section 2.8, and Exercise 76, page 89)

MT313:Discrete Mathematics

Subject Code	MT313	Credit: 6 (L-T-P: 5-1-0)
Subject Name	Discrete Mathematics	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Ordered Sets

(Lectures: 10)

Definitions, Examples and basic properties of ordered sets, Order isomorphism, Hasse diagrams, Dual of an ordered set, Duality principle, Maximal and minimal elements, Building new ordered sets, Maps between ordered sets.

Unit 2: Lattices

(Lectures: 20)

Lattices as ordered sets, Lattices as algebraic structures, Sublattices, Products and homomorphisms; Definitions, Examples and properties of modular and distributive lattices, The $M_3 - N_5$ Theorem with applications, Complemented lattice, Relatively complemented lattice, Sectionally complemented lattice.

Unit 3: Boolean Algebras and Switching Circuits

(Lectures: 20)

Boolean Algebras, De Morgan's laws, Boolean homomorphism, Representation theorem; Boolean polynomials, Boolean polynomial functions, Disjunctive normal form and conjunctive normal form, Minimal forms of Boolean polynomial, Quinn-McCluskey method, Karnaugh diagrams, Switching circuits and applications of switching circuits.

Unit 4: Graph Theory

(Lectures: 20)

Introduction to graphs, Konigsberg Bridge problem, Instant insanity game; Definition, examples and basic properties of graphs, Subgraphs, Pseudographs, Complete graphs, Bipartite graphs, Isomorphism of graphs, Paths and circuits, Eulerian circuits, Hamiltonian cycles, Adjacency matrix, Weighted graph, Travelling salesman problem, Shortest path, Dijkstra's algorithm.

References:

1. Davey, B. A., & Priestley, H. A. (2002). *Introduction to lattices and order* (2nd ed.). Cambridge University press, Cambridge.
2. Goodaire, Edgar G., & Parmenter, Michael M. (2011). *Discrete Mathematics with graph theory* (3rd ed.). Pearson Education (Singapore) Pvt. Ltd. Indian Reprint.
3. Lidl, Rudolf & Pilz, Gunter. (2004). *Applied Abstract Algebra* (2nd ed.), Undergraduate Texts in Mathematics. Springer (SIE). Indian Reprint.
4. Rosen, Kenneth H. (2012). *Discrete Mathematics and its applications, with combinatorics and graph theory*. (7th ed.). McGraw Hill Education. Indian Reprint.

Teaching Plan (MT313: Discrete Mathematics):

Weeks 1 and 2: Definitions, Examples and basic properties of ordered sets, Order isomorphism, Hasse diagrams, dual of an ordered set, Duality principle, Maximal and minimal elements, Building new ordered sets, Maps between ordered sets.

[1] Chapter 1 (Sections 1.1 to 1.5 and 1.14 to 1.26, and 1.34 to 1.36)

[3] Chapter 1 [Section 1 (1.1 to 1.3)]

Weeks 3 and 4: Lattices as ordered sets, Lattices as algebraic structures, Sublattices, Products and homomorphisms.

[1] Chapter 2 (Sections 2.1 to 2.19)

[3] Chapter 1 [Section 1 (1.5 to 1.20)]

Week 5: Definitions, Examples and properties of Modular and Distributive lattices.

[1] Chapter 4 (Sections 4.1 to 4.9)

[3] Chapter 1 [Section 2 (2.1 to 2.6)].

Week 6: M3–N5 Theorem with applications, Complemented lattice, Relatively complemented lattice, sectionally complemented lattice.

[1] Chapter 4 (Sections 4.10, and 4.11)

[3] Chapter 1 [Section 2 (2.7 to 2.14)]

Weeks 7 and 8: Boolean Algebras, De Morgan's laws, Boolean homomorphism, representation theorem. Boolean polynomials, Boolean polynomial functions, Disjunctive normal form and conjunctive normal form.

[3] Chapter 1 (Sections 3, and 4)

Week 9: Minimal forms of Boolean polynomial, Quinn-McCluskey method, Karnaugh diagrams. [3] Chapter 1 (Section 6)

Week 10: Switching circuits and applications of switching circuits.

[3] Chapter 2 (Sections 7, and 8).

Weeks 11 and 12: Introduction to graphs, Königsberg Bridge problem, Instant insanity game. Definition, Examples and basic properties of graphs, Subgraphs, Pseudographs, Complete graphs, Bipartite graphs, Isomorphism of graphs.

[2] Chapter 9 [Sections 9.1, 9.2 (9.2.1, 9.2.7), and 9.3]

Weeks 13 and 14: Paths and circuits, Eulerian circuits, Hamiltonian cycles, Adjacency matrix, Weighted graph, Travelling salesman problem, shortest path, Dijkstra's algorithm.

[2] Chapter 10 [Sections 10.1 to 10.4 (10.4.1 to 10.4.3)]

MT315: Cryptography and Network Security

Subject Code	MT315	Credit: 6 (L-T-P: 5-1-0)
Subject Name	Cryptography and Network Security	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Cryptography and Data Encryption Standard (DES) (Lectures: 20)

Overview of Cryptography, Computer security concepts, Security attacks, Symmetric cipher model, Cryptanalysis and brute-force attack, Substitution techniques, Caesar cipher, Monoalphabetic ciphers, Playfair cipher, Hill cipher, Polyalphabetic ciphers, One-time pad, Transposition techniques, Binary and ASCII, Pseudo-random bit generation, Stream ciphers and Block ciphers, The Feistel cipher, The data encryption standard (DES), DES example.

Unit 2: Algorithms and Advanced Encryption Standard (AES) (Lectures: 20)

Review of basic concepts in Number theory and Finite Fields: Divisibility, Polynomial and modular arithmetic, Fermat's and Euler's theorems, The Chinese remainder theorem, Discrete logarithm., Finite fields of the form $GF(p)$ and $GF(2^n)$. Advanced encryption standard (AES), AES transformation functions, AES key expansion, AES example.

Unit 3: Public-key Cryptography (Lectures: 15)

Principles of public-key cryptosystems, The RSA algorithm and security of RSA, Elliptic curve arithmetic, Elliptic curve cryptography, Cryptographic Hash functions, Secure Hash algorithm.

Unit 4: Digital Signatures and Network Security (Lectures: 15)

Digital signatures, Elgamal and Schnorr digital signature schemes, Digital signature algorithm. Wireless network and mobile device security, Email architecture, formats, threats and security, Secure/Multipurpose Internet Mail Extension (S/MIME) and Pretty Good Privacy (PGP).

References:

1. Stallings, William (2017). *Cryptography and Network Security, Principles and Practice* (7th ed.). Pearson Education Limited. England.
2. Trappe, Wade & Washington, Lawrence C. (2006). *Introduction to Cryptography with Coding Theory* (2nd ed.). Pearson Education International.

Additional Reading:

1. Stinson, Douglas R. (2005). *Cryptography Theory and Practice* (3rd ed.). CRC Press.

Teaching Plan (MT315: Cryptography and Network Security):

Weeks 1 and 2: Overview of Cryptography, Computer security concepts, Security attacks, Symmetric cipher model, Cryptanalysis and brute-force attack, Substitution techniques, Caesar cipher, Monoalphabetic ciphers, Playfair cipher, Hill cipher, Polyalphabetic ciphers, One-time pad.

[2] Chapter 1

[1] Chapter 1 (Sections 1.1, and 1.3), Chapter 3 (Sections 3.1, 3.2)

Weeks 3 and 4: Transposition techniques, Binary and ASCII, Pseudo-random bit generation, Stream ciphers and Block ciphers, The Feistel cipher, The Data Encryption Standard (DES), DES example.

[1] Chapter 3 (Section 3.3), and Chapter 4 (Sections 4.1 to 4.3)

[2] Chapter 2 (Sections 2.8, and 2.10)

Weeks 5 and 6: Review of basic concepts in Number theory and Finite Fields: Divisibility, Polynomial and modular arithmetic, Statements of Fermat's and Euler's theorems, The Chinese remainder theorem, Discrete logarithm, Finite fields of the form $GF(p)$ and $GF(2^n)$.

[1] Chapter 1 (Sections 2.1 to 2.3, 2.5, 2.7, and 2.8), and Chapter 5 (Sections 5.4 to 5.6)

Weeks 7 and 8: Advanced encryption standard (AES), AES transformation functions, AES key expansion, AES example.

[1] Chapter 6 [Sections 6.1 to 6.5 (up to page 195)]

Weeks 9 and 10: Principles of public-key cryptosystems, The RSA algorithm and security of RSA, Elliptic curve arithmetic, Elliptic curve cryptography.

[1] Chapter 9 (Sections 9.1, and 9.2), and Chapter 10 (Sections 10.3, and 10.4)

Week 11: Cryptographic Hash functions, Secure Hash algorithm.

[1] Chapter 11 (Sections 11.1, and 11.5)

Weeks 12 and 13: Digital signatures, Elgamal and Schnorr digital signature schemes, The digital signature algorithm. Wireless network and mobile device security.

[1] Chapter 13 (Sections 13.1 to 13.4), and Chapter 18 (Sections 18.1, and 18.2)

Week 14: Email architecture, threats and security, Secure/Multipurpose Internet Mail Extension (S/MIME) and Pretty Good Privacy (PGP).

[1] Chapter 19 [Sections 19.1 to 19.5 (Confidentiality excluded)]

Semester VI

Subject Code	MT302	Credit: 4 (L-T-P: 4-0-2) 4 Lecture (per week) 4 Hours Practical (per week per student)
Subject Name	Complex Analysis	
Total Marks	150 (Theory:70, Internal Assessment: 30, Practical: 50)	
Examination	3 Hours (Written) + 2 Hours (Practical)	

Unit 1: Analytic Functions and Cauchy-Riemann Equations (Lectures: 16)

Functions of complex variable, Mappings; Mappings by the exponential function, Limits, Theorems on limits, Limits involving the point at infinity, Continuity, Derivatives, Differentiation formulae, Cauchy-Riemann equations, Sufficient conditions for differentiability; Analytic functions and their examples.

Unit 2: Elementary Functions and Integrals (Lectures: 14)

Exponential function, Logarithmic function, Branches and derivatives of logarithms, Trigonometric function, Derivatives of functions, Definite integrals of functions, Contours, Contour integrals and its examples, Upper bounds for moduli of contour integrals,

Unit 3: Cauchy's Theorems and Fundamental Theorem of Algebra (Lectures: 12)

Antiderivatives, Proof of antiderivative theorem, Cauchy-Goursat theorem, Cauchy integral formula; An extension of Cauchy integral formula, Consequences of Cauchy integral formula, Liouville's theorem and the fundamental theorem of algebra.

Unit 4: Series and Residues (Lectures: 14)

Convergence of sequences and series, Taylor series and its examples; Laurent series and its examples, Absolute and uniform convergence of power series, Uniqueness of series representations of power series, Isolated singular points, Residues, Cauchy's residue theorem, residue at infinity; Types of isolated singular points, Residues at poles and its examples.

Reference:

1. Brown, James Ward, & Churchill, Ruel V. (2014). *Complex Variables and Applications* (9th ed.). McGraw-Hill Education. New York.

Additional Readings:

1. Bak, Joseph & Newman, Donald J. (2010). *Complex analysis* (3rd ed.). Undergraduate Texts in Mathematics, Springer. New York.
2. Zills, Dennis G., & Shanahan, Patrick D. (2003). *A First Course in Complex Analysis with Applications*. Jones & Bartlett Publishers, Inc.
3. Mathews, John H., & Howell, Russell W. (2012). *Complex Analysis for Mathematics and Engineering* (6th ed.). Jones & Bartlett Learning. Narosa, Delhi. Indian Edition. (For practicals: Sample materials of files in the form Mathematica/Maple 2011.zip, log to: www.jblearning.com/catalog/9781449604455/).

Teaching Plan (Theory of MT302: Complex Analysis):

Week 1: Functions of complex variable, Mappings, Mappings by the exponential function.[1] Chapter 2 (Sections 12 to 14)

Week 2: Limits, Theorems on limits, Limits involving the point at infinity, Continuity.[1] Chapter 2 (Sections 15 to 18)

Week 3: Derivatives, Differentiation formulae, Cauchy-Riemann equations, Sufficient conditions for Differentiability.
[1] Chapter 2 (Sections 19 to 22)

Week 4: Analytic functions, Examples of analytic functions, Exponential function.[1] Chapter 2 (Sections 24, and 25), and Chapter 3 (Section 29)

Week 5: Logarithmic function, Branches and Derivatives of Logarithms, Trigonometric functions.[1] Chapter 3 (Sections 30, 31, and 34)

Week 6: Derivatives of functions, Definite integrals of functions, Contours.
[1] Chapter 4 (Sections 37 to 39)

Week 7: Contour integrals and its examples, upper bounds for moduli of contour integrals.
[1] Chapter 4 (Sections 40, 41, and 43).

Week 8: Antiderivatives, proof of antiderivative theorem.
[1] Chapter 4 (Sections 44, and 45)

Week 9: State Cauchy-Goursat theorem, Cauchy integral formula.
[1] Chapter 4 (Sections 46, and 50)

Week 10: An extension of Cauchy integral formula, Consequences of Cauchy integral formula, Liouville's theorem and the fundamental theorem of algebra.
[1] Chapter 4 (Sections 51 to 53)

Week 11: Convergence of sequences, Convergence of series, Taylor series, proof of Taylor's theorem, Examples.
[1] Chapter 5 (Sections 55 to 59)

Week 12: Laurent series and its examples, Absolute and uniform convergence of power series, uniqueness of series representations of power series.
[1] Chapter 5 (Sections 60, 62, 63, and 66).

Week 13: Isolated singular points, Residues, Cauchy's residue theorem, Residue at infinity. [1]:
Chapter 6 (Sections 68 to 71)

Week 14: Types of isolated singular points, Residues at poles and its examples.
[1] Chapter 6 (Sections 72 to 74)

Practical / Lab work to be performed in Computer Lab:

Modeling of the following problems using Mathematica /Maple/MATLAB /Maxima/Scilab etc.

1. Make a geometric plot to show that the n^{th} roots of unity are equally spaced points that lie on the unit circle $C_1(0) = \{z : |z| = 1\}$ and form the vertices of a regular polygon with n sides, for $n = 4, 5, 6, 7, 8$.
2. Find all the solutions of the equation $z^3 = 8i$ and represent these geometrically.
3. Write parametric equations and make a parametric plot for an ellipse centered at the origin with horizontal major axis of 4 units and vertical minor axis of 2 units. Show the effect of rotation of this ellipse by an angle of $\frac{\pi}{6}$ radians and shifting of the centre from $(0,0)$ to $(2,1)$, by making a parametric plot.
4. Show that the image of the open disk $D_1(-1-i) = \{z : |z+1+i| < 1\}$ under the linear transformation $w = f(z) = (3-4i)z + 6 + 2i$ is the open disk:

$$D_5(-1+3i) = \{w : |w+1-3i| < 5\}.$$
5. Show that the image of the right half plane $\text{Re } z = x > 1$ under the linear transformation $w = (-1+i)z - 2 + 3i$ is the half plane $v > u + 7$, where $u = \text{Re}(w)$, etc. Plot the map.
6. Show that the image of the right half plane $A = \left\{z : \text{Re } z \geq \frac{1}{2}\right\}$ under the mapping $w = f(z) = \frac{1}{z}$ is the closed disk $\overline{D_1(1)} = \{w : |w-1| \leq 1\}$ in the w - plane.
7. Make a plot of the vertical lines $x = a$, for $a = -1, -\frac{1}{2}, \frac{1}{2}, 1$ and the horizontal lines $y = b$, for $b = -1, -\frac{1}{2}, \frac{1}{2}, 1$. Find the plot of this grid under the mapping $w = f(z) = \frac{1}{z}$.
8. Find a parametrization of the polygonal path $C = C_1 + C_2 + C_3$ from $-1+i$ to $3-i$, where C_1 is the line from: $-1+i$ to -1 , C_2 is the line from: -1 to $1+i$ and C_3 is the line from $1+i$ to $3-i$. Make a plot of this path.
9. Plot the line segment 'L' joining the point $A = 0$ to $B = 2 + i\frac{\pi}{4}$ and give an exact calculation of $\int_L e^z dz$.
10. Plot the semicircle 'C' with radius 1 centered at $z = 2$ and evaluate the contour integral $\int_C \frac{1}{z-2} dz$.

11. Show that $\int_{C_1} z dz = \int_{C_2} z dz = 4 + 2i$, where C_1 is the line segment from $-1 - i$ to $3 + i$ and C_2 is the portion of the parabola $x = y^2 + 2y$ joining $-1 - i$ to $3 + i$. Make plots of two contours C_1 and C_2 joining $-1 - i$ to $3 + i$.
12. Use ML inequality to show that $\left| \int_C \frac{1}{z^2 + 1} dz \right| \leq \frac{1}{2\sqrt{5}}$, where C is the straight line segment from 2 to $2 + i$. While solving, represent the distance from the point z to the points i and $-i$, respectively, i.e. $|z - i|$ and $|z + i|$ on the complex plane \square .
13. Show that $\int_C \frac{dz}{2z^{1/2}}$, where $z^{1/2}$ is the principal branch of the square root function and C is the line segment joining 4 to $8 + 6i$. Also plot the path of integration.
14. Find and plot three different Laurent series representations for the function $f(z) = \frac{3}{2 + z - z^2}$, involving powers of z .
15. Locate the poles of $f(z) = \frac{1}{5z^4 + 26z^2 + 5}$ and specify their order.
16. Locate the zeros and poles of $g(z) = \frac{\pi \cot(\pi z)}{z^2}$ and determine their order. Also justify that $\text{Res}(g, 0) = -\frac{\pi^2}{3}$.
17. Evaluate $\int_{C_1^+(0)} \exp\left(\frac{2}{z}\right) dz$, where $C_1^+(0)$ denotes the circle: $\{z : |z| = 1\}$ with positive orientation. Similarly evaluate $\int_{C_3^+(0)} \frac{1}{z^4 + z^3 - 2z^2} dz$.

Subject Code	MT304	Credit: 6 (L-T-P: 5-1-0) 5 Lecture (per week) 1 Tutorial (per week per student)
Subject Name	Ring Theory and Linear Algebra-II	
Total Marks	100 (Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Polynomial Rings and Unique Factorization Domain (UFD) (Lectures: 25)

Polynomial rings over commutative rings, Division algorithm and consequences, Principal ideal domains, Factorization of polynomials, Reducibility tests, Irreducibility tests, Eisenstein criterion, Unique factorization in $\mathbb{Z}[x]$; Divisibility in integral domains, Irreducibles, Primes, Unique factorization domains, Euclidean domains.

Unit 2: Dual Spaces and Diagonalizable Operators (Lectures: 15)

Dual spaces, Double dual, Dual basis, Transpose of a linear transformation and its matrix in the dual basis, Annihilators; Eigenvalues, Eigenvectors, Eigenspaces and characteristic polynomial of a linear operator; Diagonalizability, Invariant subspaces and Cayley-Hamilton theorem; The minimal polynomial for a linear operator.

Unit 3: Inner Product Spaces (Lectures: 15)

Inner product spaces and norms, Orthonormal basis, Gram-Schmidt orthogonalization process, Orthogonal complements, Bessel's inequality.

Unit 4: Adjoint Operators and Their Properties (Lectures: 15)

The adjoint of a linear operator, Least squares approximation, Minimal solutions to systems of linear equations, Normal, Self-adjoint, Unitary and orthogonal operators and their properties.

References:

1. Friedberg, Stephen H., Insel, Arnold J., & Spence, Lawrence E. (2003). *Linear Algebra* (4th ed.). Prentice-Hall of India Pvt. Ltd. New Delhi.
2. Gallian, Joseph. A. (2013). *Contemporary Abstract Algebra* (8th ed.). Cengage Learning India Private Limited. Delhi. Fourth impression, 2015.

Additional Readings:

1. Herstein, I. N. (2006). *Topics in Algebra* (2nd ed.). Wiley Student Edition. India.
2. Hoffman, Kenneth, & Kunze, Ray Alden (1978). *Linear Algebra* (2nd ed.). Prentice-Hall of India Pvt. Limited. Delhi. Pearson Education India Reprint, 2015.
3. Lang, Serge (1987). *Linear Algebra* (3rd ed.). Springer.

Teaching Plan (MT304: Ring Theory and Linear Algebra-II):

Week 1: Polynomial rings over commutative rings, Division algorithm and consequences, Principalideal domains.

[2] Chapter 16

Weeks 2 and 3: Factorization of polynomials, Reducibility tests, Irreducibility tests, Eisenstein's criterion, Unique factorization in $\mathbb{Z}[x]$.

[2] Chapter 17

Weeks 4 and 5: Divisibility in integral domains, Irreducibles, Primes, Unique factorization domains, Euclidean domains.

[2] Chapter 18

Week 6: Dual spaces, Double dual, Dual basis, Transpose of a linear transformation and its matrix in the dual basis, Annihilators.

[1] Chapter 2 (Section 2.6)

Weeks 7 and 8: Eigenvalues, Eigenvectors, Eigenspaces and characteristic polynomial of a linear operator; Diagonalizability, Invariant subspaces and Cayley-Hamilton theorem; The minimal polynomial for a linear operator.

[1] Chapter 5 (Sections 5.1, 5.2, and 5.4), and Chapter 7 (Section 7.3, Statement of Theorem 7.16)

Week 9: Inner product spaces and norms.

[1] Chapter 6 (Section 6.1)

Weeks 10 and 11: Orthonormal basis, Gram-Schmidt orthogonalization process, Orthogonal complements, Bessel's inequality.

[1] Chapter 6 (Section 6.2)

Week 12: The adjoint of a linear operator and its properties, Least squares approximation, Minimal solutions to systems of linear equations.

[1] Chapter 6 (Section 6.3, Statement of Theorem 6.13 with applications)

Weeks 13 and 14: Normal, Self-adjoint, unitary and orthogonal operators and their properties. [1] Chapter 6 (Sections 6.4, and 6.5, up to Theorem 6.21, page 385)

Discipline Specific Elective (DSE) Course - 3

Any one of the following (at least two shall be offered by the college):

MT306	Mathematical Finance
MT308	Introduction to Information Theory and Coding
MT310	Biomathematics

Subject Code	MT306	Credit: 6 (L-T-P : 5-1-0)
Subject Name	Mathematical Finance	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Interest Rates

(Lectures: 20)

Interest rates, Types of rates, Measuring interest rates, Zero rates, Bond pricing, Forward rate, Duration, Convexity, Exchange traded markets and OTC markets, Derivatives--Forward contracts, Futures contract, Options, Types of traders, Hedging, Speculation, Arbitrage.

Unit 2: Mechanics and Properties of Options

(Lectures: 15)

No Arbitrage principle, Short selling, Forward price for an investment asset, Types of Options, Option positions, Underlying assets, Factors affecting option prices, Bounds on option prices, Put-call parity, Early exercise, Effect of dividends.

Unit 3: Stochastic Analysis of Stock Prices and Black-Scholes Model

(Lectures: 20)

Binomial option pricing model, Risk neutral valuation (for European and American options on assets following binomial tree model), Lognormal property of stock prices, Distribution of rate of return, expected return, Volatility, estimating volatility from historical data, Extension of risk neutral valuation to assets following GBM, Black-Scholes formula for European options.

Unit 4: Hedging Parameters, Trading Strategies and Swaps

(Lectures: 15)

Hedging parameters (the Greeks: Delta, Gamma, Theta, Rho and Vega), Trading strategies involving options, Swaps, Mechanics of interest rate swaps, Comparative advantage argument, Valuation of interest rate swaps, Currency swaps, Valuation of currency swaps.

Reference:

1. Hull, J. C., & Basu, S. (2010). *Options, Futures and Other Derivatives* (7th ed.). Pearson Education. New Delhi.

Additional Readings:

1. Luenberger, David G. (1998). *Investment Science*, Oxford University Press. Delhi.
2. Ross, Sheldon M. (2011). *An elementary Introduction to Mathematical Finance* (3rd ed.). Cambridge University Press. USA.

Teaching Plan (MT306: Mathematical Finance):

Weeks 1 and 2: Interest rates, Types of rates, measuring interest rates, zero rates, Bond pricing, Forward rate, Duration, Convexity.

[1] Chapter 4 (Section 4.1 to 4.4, 4.6, 4.8, and 4.9)

Weeks 3 and 4: Exchange Traded Markets and OTC markets, Derivatives- Forward contracts, Futures contract, Options, Types of traders, Hedging, Speculation, Arbitrage [1] Chapter 1 (Sections 1.1 to 1.9)

Week 5: No Arbitrage principle, Short selling, Forward price for an investment asset. [1] Chapter 5 (Sections 5.2 to 5.4)

Week 6: Types of Options, Option positions, Underlying assets, Factors affecting option prices. [1] Chapter 8 (Sections 8.1 to 8.3), and Chapter 9 (Section 9.1)

Week 7: Bounds on option prices, Put-call parity, Early exercise, Effect of dividends. [1] Chapter 9 (Sections 9.2 to 9.7)

Week 8: Binomial option pricing model, Risk neutral Valuation (for European and American options on assets following binomial tree model).

[1] Chapter 11 (Sections 11.1 to 11.5)

Weeks 9 to 11: Lognormal property of stock prices, Distribution of rate of return, expected return, Volatility, estimating volatility from historical data. Extension of risk neutral valuation to assets following GBM (without proof), Black-Scholes formula for European options.

[1] Chapter 13 (Sections 13.1 to 13.4, 13.7, and 13.8)

Week 12: Hedging parameters (the Greeks: Delta, Gamma, Theta, Rho and Vega). [1] Chapter 17 (Sections 17.1 to 17.9)

Week 13: Trading strategies Involving options.

[1] Chapter 10 (except box spreads, calendar spreads and diagonal spreads)

Week 14: Swaps, Mechanics of interest rate swaps, Comparative advantage argument, Valuation of interest rate swaps, Currency swaps, Valuation of currency swaps [1] Chapter 7 (Sections 7.1 to 7.4, and 7.7 to 7.9)

Subject Code	MT308	Credit: 6 (L-T-P: 5-1-0)
Subject Name	Introduction to Information Theory and Coding	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Concepts of Information Theory

(Lectures: 20)

Communication processes, A model of communication system, A quantitative measure of information, Binary unit of information, A measure of uncertainty, H function as a measure of uncertainty, Sources and binary sources, Measure of information for two-dimensional discrete finite probability schemes.

Unit 2: Entropy Function

(Lectures: 20)

A sketch of communication network, Entropy, Basic relationship among different entropies, A measure of mutual information, Interpretation of Shannon's fundamental inequalities; Redundancy, Efficiency and channel capacity, Binary symmetric channel, Binary erasure channel, Uniqueness of the entropy function, Joint entropy and conditional entropy, Relative entropy and mutual information, Chain rules for entropy, Conditional relative entropy and conditional mutual information, Jensen's inequality and its characterizations, The log sum inequality and its applications.

Unit 3: Concepts of Coding

(Lectures: 15)

Block codes, Hamming distance, Maximum likelihood decoding, Levels of error handling, Error correction, Error detection, Erasure correction, Construction of finite fields, Linear codes, Matrix representation of linear codes.

Unit 4: Bounds of Codes

(Lectures: 15)

Orthogonality relation, Encoding of linear codes, Decoding of linear codes, The singleton bound and maximum distance separable codes, The sphere-packing bound and perfect codes, The Gilbert-Varshamov bound, MacWilliams' identities.

References:

1. Cover, Thomas M., & Thomas, Joy A. (2006). *Elements of Information Theory* (2nd ed.). Wiley India. Indian Reprint 2014.
2. Gallian, Joseph. A. (2013). *Contemporary Abstract Algebra*(8th ed.).Cengage Learning India Private Limited. Delhi. Fourth impression, 2015.
3. Reza, Fazlollah M. (1961). *An Introduction to Information Theory*. Dover Publications Inc, New York. Reprint 1994.
4. Roth, Ron M. (2007). *Introduction to Coding Theory*. Cambridge University Press.

Teaching Plan MT 308(ii): Introduction to Information Theory and Coding:

Weeks 1 and 2: Communication processes, A model of communication system, A quantitative measure of information, Binary unit of information.

[3] Chapter 1 (Sections 1.1 to 1.7)

Weeks 3 and 4: A measure of uncertainty, H function as a measure of uncertainty, Sources and binary sources, Measure of information for two-dimensional discrete finite probability schemes.

[3] Chapter 3 (Sections 3.1 to 3.7)

Weeks 5 and 6: A sketch of communication network, Entropy, Basic relationship among different entropies, A measure of mutual information, Interpretation of Shannon's fundamental inequalities; redundancy, efficiency and channel capacity, Binary symmetric channel, Binary erasure channel, Uniqueness of the entropy function.

[3] Chapter 3 (Sections 3.9, 3.11 to 3.16, and 3.19)

[1] Chapter 2 (Section 2.1)

Weeks 7 and 8: Joint entropy and conditional entropy, Relative entropy and mutual information, Chain rules for entropy, Conditional relative entropy and conditional mutual information, Jensen's inequality and its characterizations, The log sum inequality and its applications.

[1] Chapter 2 (Sections 2.2 to 2.7)

Weeks 9 and 10: Block codes, Hamming distance, Maximum likelihood decoding, Levels of error handling, Error correction, Error detection, Erasure correction, Construction of finite fields.

[4] Chapter 1 (Sections 1.2 to 1.5, excluding 1.5.3), and Chapter 3 (Sections 3.1 to 3.4)

Weeks 11 and 12: Linear codes, Matrix representation of linear codes, Orthogonality relation, Encoding of linear codes, Decoding of linear codes.

[4] Chapter 2 (Sections 2.1 to 2.4)

[2] Chapter 31 (Lemma and Theorem 31.3 on page 538)

Weeks 13 and 14: The singleton bound and maximum distance separable codes, The sphere-packing bound and perfect codes, the Gilbert-Varshamov bound, MacWilliams' identities.

[4] Chapter 4 (Sections 4.1 to 4.4), and Chapter 11 (Section 11.1)

Subject Code	MT310	Credit: 6 (L-T-P: 5-1-0)
Subject Name	Biomathematics	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Modeling Biological Phenomenon

(Lectures: 14)

Population growth, Administration of drugs, differential equations, Heartbeat, Nerve impulse prey models.

Unit 2: Mathematics of Heart Physiology and Nerve Impulse Transmission

(Lectures: 28)

Stability and oscillations: Epidemics, The phase plane and the Jacobian matrix, Local stability, Stability, Limit cycles, Forced oscillations; Mathematics of Heart Physiology: The local model, The Threshold effect, The phase plane analysis and the heartbeat model, A model of the cardiac pacemaker; Mathematics of Nerve Impulse Transmission: Excitability and repetitive firing, Travelling waves.

Unit 3: Bifurcation and Chaos

(Lectures: 13)

Bifurcation, Bifurcation of a limit cycle, Discrete bifurcation and period-doubling, Chaos, Stability of limit cycles, The Poincaré plane.

Unit 4: Modeling Molecular Evolution and Genetics

(Lectures: 15)

Modelling Molecular Evolution: Matrix models of base substitutions for DNA sequences, The Jukes-Cantor model, The Kimura models, Phylogenetic distances; Constructing Phylogenetic Trees: Phylogenetic trees, Unweighted pair-group method with arithmetic means (UPGMA), Neighbor joining method; Genetics: Mendelian genetics, Probability distributions in genetics.

References:

1. Allman, Elizabeth S., & Rhodes, John A. (2004). *Mathematical Models in Biology: An Introduction*. Cambridge University Press.
2. Jones, D. S., Plank, M. J., & Sleeman, B. D. (2009). *Differential Equations and Mathematical Biology* (2nd ed.). CRC Press, Taylor & Francis Group, LLC.

Additional Readings:

1. Murray, J. D. (2002). *An Introduction to Mathematical Biology* (3rd ed.). Springer.
2. Myint-U, Tyn (1977). *Ordinary Differential Equation*. Elsevier North-Holland, Inc.
3. Simmons, George F., & Krantz, Steven G. (2015). *Differential Equations*. McGraw-Hill Education. Indian Reprint.
4. Strogatz, Steven H. (2009). *Nonlinear Dynamics and Chaos* (2nd ed.). Perseus Book Publishing. LLC. Sarat Publication, Kolkata, India.

Teaching Plan (MT310 : Biomathematics):

Week 1: Population growth, Administration of drugs, Cell division, Systems of linear ordinary differential equations.

[2] Chapter 1 (Sections 1.1 to 1.3), and Chapter 3 (An overview of the methods in Sections 3.1 to 3.6)

Week 2: Heartbeat, Nerve impulse transmission

[2] Chapter 4 (Sections 4.2, and 4.3)

Week 3: Chemical reactions, Predator-prey models, Epidemics (Mathematical model). [2] Chapter 4 (Sections 4.4, and 4.5), and Chapter 5 (Section 5.2)

Week 4: The phase plane and Jacobian matrix, Local stability.

[2] Chapter 5 (Sections 5.3, and 5.4)

Week 5: Stability, Limit cycles.

[2] Chapter 5 [Sections 5.5, and 5.6 (up to page number 137)]

Week 6: Limit cycle criterion and Poincaré-Bendixson Theorem (interpretation only, with Example 5.6.1), Forced oscillations.

[2] Chapter 5 [Section 5.6 (Page number 137 to 138), and Section 5.7)

Week 7: Mathematics of Heart Physiology: The local model, The Threshold effect, The phase plane analysis and the heartbeat model.

[2] Chapter 6 (Sections 6.1 to 6.3)

Week 8: A model of the cardiac pacemaker, Excitability and repetitive firing.

[2] Chapter 6 (Section 6.5), and Chapter 7 (Section 7.1)

Week 9: Travelling waves, Bifurcation, Bifurcation of a limit

cycle. [2] Chapter 7 (Section 7.2), and Chapter 13 (Sections 13.1, and 13.2)

Weeks 10 and 11: Discrete bifurcation and period-doubling, Chaos, Stability of limit cycles, The Poincaré plane.

[2] Chapter 13 (Sections 13.3 to 13.6)

Week 12: Matrix models of base substitutions for DNA sequences, The Jukes-Cantor model, The Kimura models, Phylogenetic distances.

[1] Chapter 4 (Sections 4.4, and 4.5)

Week 13: Constructing Phylogenetic Trees: Phylogenetic trees, Unweighted pair-group method with arithmetic means (UPGMA), Neighbor joining method.

[1] Chapter 5 (Sections 5.1 to 5.3)

Week 14: Genetics: Mendelian Genetics, Probability distributions in Genetics.

[1] Chapter 6 [Sections 6.1, and 6.2 (up to Equation 6.2 only)]

Discipline Specific Elective (DSE) Course - 4

Any one of the following (at least *two* shall be offered by the college):

MT312: Number Theory

MT314: Linear Programming and Applications

MT316: Mechanics

Subject Code	MT312	Credit: 6 (L-T-P: 5-1-0)
Subject Name	Number Theory	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Distribution of Primes and Theory of Congruencies (Lectures: 15)

Linear Diophantine equation, Prime counting function, Prime number theorem, Goldbach conjecture, Fermat and Mersenne primes, Congruence relation and its properties, Linear congruence and Chinese remainder theorem, Fermat's little theorem, Wilson's theorem.

Unit 2: Number Theoretic Functions (Lectures: 15)

Number theoretic functions for sum and number of divisors, Multiplicative function, The Mobius inversion formula, The greatest integer function. Euler's phi-function and properties, Euler's theorem.

Unit 3: Primitive Roots (Lectures: 20)

The order of an integer modulo n , Primitive roots for primes, Composite numbers having primitive roots; Definition of quadratic residue of an odd prime, and Euler's criterion.

Unit 4: Quadratic Reciprocity Law and Public Key Encryption (Lectures: 20)

The Legendre symbol and its properties, Quadratic reciprocity, Quadratic congruencies with composite moduli; Public key encryption, RSA encryption and decryption.

References:

1. Burton, David M. (2007). *Elementary Number Theory* (7th ed.). Tata Mc-Graw Hill Edition, Indian Reprint.
2. Jones, G. A., & Jones, J. Mary. (2005). *Elementary Number Theory*. Undergraduate Mathematics Series (SUMS). First Indian Print.

Additional Reading:

1. Neville Robinns. (2007). *Beginning Number Theory* (2nd ed.). Narosa Publishing House Pvt. Limited, Delhi.

Teaching Plan (MT312: Number Theory):

Week 1 : Linear Diophantine equation and its solutions, Distribution of primes, Prime counting function, Statement of the prime number theorem, Goldbach conjecture.

[1] Chapter 2 (Section 2.5)

[2] Chapter 2 (Section 2.2)

Week 2: Fermat and Mersenne primes, Congruence relation and its basic properties, Linear congruence equation and its solutions.

[2] Chapter 2 (Section 2.3)

[1] Chapter 4 (Sections 4.2, and 4.4)

Week 3: Chinese remainder theorem, to solve system of linear congruence for two variables, Fermat's little theorem, Wilson's theorem.

[1] Chapter 4 (Section 4.4), Chapter 5 (Section 5.2 up to before pseudo-prime at page 90, Section 5.3)

Weeks 4 and 5: Number theoretic functions for sum and number of divisors, Multiplicative function, and the Mobius inversion formula. The greatest integer function, Euler's phi-function.

[1] Chapter 6 (Sections 6.1 to 6.2), and Chapter 7 (Section 7.2)

Week 6: Euler's theorem, Properties of Euler's phi-function.

[1] Chapter 7 (Sections 7.3, and 7.4)

Weeks 7 and 8: The order of an integer modulo n . Primitive roots for primes.

[1] Chapter 8 (Sections 8.1, and 8.2)

Week 9: Composite numbers having primitive roots.

[1] Chapter 8 (Section 8.3)

Week 10: Definition of quadratic residue of an odd prime, and Euler's criterion.

[1] Chapter 9 (Section 9.1)

Weeks 11 and 12: The Legendre symbol and its properties. Quadratic reciprocity law. [1] Chapter 9 (Section 9.2 up to page 181, and Section 9.3)

Week 13: Quadratic congruencies with composite moduli.

[1] Chapter 9 (Section 9.4)

Week 14: Public key encryption, RSA encryption and decryption scheme.

[1] Chapter 10 (Section 10.1)

Subject Code	MT314	Credit: 6 (L-T-P: 5-1-0)
Subject Name	Linear Programming and Applications	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Introduction to Linear Programming

(Lectures: 15)

The Linear Programming Problem: Standard, Canonical and matrix forms, Graphical solution. Hyperplanes, Extreme points, Convex and polyhedral sets. Basic solutions; Basic Feasible Solutions; Reduction of any feasible solution to a basic feasible solution; Correspondence between basic feasible solutions and extreme points.

Unit 2: Methods of Solving Linear Programming Problem

(Lectures: 25)

Simplex Method: Optimal solution, Termination criteria for optimal solution of the Linear Programming Problem, Unique and alternate optimal solutions, Unboundedness; Simplex Algorithm and its Tableau Format; Artificial variables, Two-phase method, Big-M method.

Unit 3: Duality Theory of Linear Programming

(Lectures: 15)

Motivation and Formulation of Dual problem; Primal-Dual relationships; Fundamental Theorem of Duality; Complimentary Slackness.

Unit 4: Applications

(Lectures: 15)

Transportation Problem: Definition and formulation; Methods of finding initial basic feasible solutions; North West corner rule. Least cost method; Vogel's Approximation method; Algorithm for solving Transportation Problem.

Assignment Problem: Mathematical formulation and Hungarian method of solving.

Game Theory: Basic concept, Formulation and solution of two-person zero-sum games, Games with mixed strategies, Linear Programming method of solving a game.

References:

1. Bazaraa, Mokhtar S., Jarvis, John J., & Sherali, Hanif D. (2010). *Linear Programming and Network Flows* (4th ed.). John Wiley and Sons.
2. Hadley, G. (1997). *Linear Programming*. Narosa Publishing House. New Delhi.
3. Taha, Hamdy A. (2010). *Operations Research: An Introduction* (9th ed.). Pearson.

Additional Readings:

1. Hillier, F. S. & Lieberman, G. J. (2010). *Introduction to Operations Research-Concepts and Cases* (9th ed.). Tata McGraw Hill.
2. Thie, Paul R., & Keough, G. E. (2014). *An Introduction to Linear Programming and Game Theory*. (3rd ed.). Wiley India Pvt. Ltd.

Teaching Plan (MT314: Linear Programming and Applications):

Week 1 : The Linear Programming Problem: Standard, Canonical and matrix forms, Graphical solution.

[1] Chapter 1 (Section 1.1)

[2] Chapter 1 (Sections 1.1 to 1.4, and 1.6)

Weeks 2 and 3: Hyperplanes, Extreme points, Convex and polyhedral sets; Basic solutions. Basic Feasible Solutions; Reduction of any feasible solution to a basic feasible solution; Correspondence between basic feasible solutions and extreme points.

[2] Chapter 2 (Sections 2.16, 2.19, and 2.20), and Chapter 3 (Sections 3.4, and 3.10)

[1] Chapter 3 (Section 3.2)

Week 4: Simplex Method: Optimal solution, Termination criteria for optimal solution of the Linear Programming Problem, Unique and alternate optimal solutions, Unboundedness.

[1] Chapter 3 (Sections 3.3, and 3.6)

Weeks 5 and 6: Simplex Algorithm and its Tableau Format.

[1] Chapter 3 (Sections 3.7, and 3.8).

Weeks 7 and 8: Artificial variables, Two-phase method, Big-M method.

[1] Chapter 4 (Sections 4.1 to 4.3)

Weeks 9 and 10: Motivation and Formulation of Dual problem; Primal-Dual relationships. [1] Chapter 6 (Section 6.1, and 6.2, up to Example 6.4)

Week 11: Statements of the Fundamental Theorem of Duality and Complementary Slackness Theorem with examples.

[1] Chapter 6 (Section 6.2)

Weeks 12 and 13: Transportation Problem. Assignment problem.

[3] Chapter 5 (Sections 5.1, 5.3, and 5.4)

Week 14: *Game Theory*: Basic concept, Formulation and solution of two-person zero-sum games, Games with mixed strategies, Linear Programming method of solving a game.

[2] Chapter 11 (Sections 11.12, and 11.13)

Subject Code	MT316	Credit: 6 (L-T-P: 5-1-0)
Subject Name	Mechanics	5 Lecture (per week) 1 Tutorial (per week per student)
Total Marks	100(Theory:70, Internal Assessment: 30)	
Examination	3 Hours (Written)	

Unit 1: Forces in Equilibrium

(Lectures: 20)

Coplanar force systems; Three-dimensional force systems; Moment of a force about a point and an axis, Principle of moments, Couple and couple moment, Moment of a couple about a line, Resultant of a force system, Distributed force system, Rigid-body equilibrium, Equilibrium of forces in two and three dimensions, Free-body diagrams, General equations of equilibrium, Constraints and statical determinacy.

Unit 2: Friction, Center of Gravity and Moments of Inertia

(Lectures: 20)

Equations of equilibrium and friction, Frictional forces on screws and flat belts; Center of gravity, Center of mass and Centroid of a body and composite bodies; Theorems of Pappus and Guldinus; Moments and products of inertia for areas, composite areas and rigid body, Parallel-axis theorem, Moment of inertia of a rigid body about an arbitrary axis, Principal moments and principal axes of inertia.

Unit 3: Conservation of Energy and Applications

(Lectures: 15)

Conservative force fields, Conservation of mechanical energy, Work-energy equations, Kinetic energy and work-kinetic energy expressions based on center of mass, Moment of momentum equation for a single particle and a system of particles.

Unit 4: Rigid Body Motion

(Lectures: 15)

Translation and rotation of rigid bodies, Chasles' Theorem, General relationship between time derivatives of a vector for different references, Relationship between velocities of a particle for different references, Acceleration of particle for different references.

References:

1. Hibbeler, R. C. (2016). *Engineering Mechanics: Statics & Dynamics* (14th ed.). Pearson Prentice Hall (Pearson Education), New Jersey.
2. Shames, Irving H., & Rao, G. Krishna Mohan (2009). *Engineering Mechanics: Statics and Dynamics* (4th ed.). Dorling Kindersley (India) Pvt. Ltd. (Pearson Education). Delhi.

Teaching Plan (MT316: Mechanics):

Weeks 1 and 2: Coplanar force systems; Three-dimensional force systems. Moment of a force about a point and an axis, Principle of moments, Couple and couple moment, Moment of a couple about a line, Resultant of a force system, Distributed force system.

[1] Chapter 3, and Chapter 4

Weeks 3 and 4: Rigid-body equilibrium, Equilibrium of forces in two and three dimensions, Free-body diagrams, General equations of equilibrium, Constraints and statical determinacy.

[1] Chapter 5

Weeks 5 and 6: Equations of equilibrium and friction, Frictional forces on screws and flat belts; Center of gravity, Center of mass and Centroid of a body and composite bodies; Theorems of Pappus and Guldinus.

[1] Chapter 8, and Chapter 9

Weeks 7 and 8: Moments and products of inertia for areas, composite areas and rigid body, Parallel-axis theorem, Moment of inertia of a rigid body about an arbitrary axis, Principal moments and principal axes of inertia.

[1] Chapter 10 (Sections 10.1 to 10.5), and Chapter 21 (Section 21.1)

Weeks 9 to 11: Conservative force fields, Conservation of mechanical energy, Work-energy equations, Kinetic energy and work-kinetic energy expressions based on center of mass, Moment of momentum equation for a single particle and a system of particles.

[2] Chapter 11, and Chapter 12 (Sections 12.5, and 12.6)

Weeks 12 to 14: Translation and rotation of rigid bodies, Chasles' Theorem, General relationship between time derivatives of a vector for different references, Relationship between velocities of a particle for different references, Acceleration of particle for different references.

[2] Chapter 13 (Sections 13.1 to 13.3, and 13.6 to 13.8)